

# Evaluation of Ionospheric Earthquake Precursor Signatures : Statistical and Tomographic Approaches over Japan Area

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4: National Central University, Taiwan

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- Introduction
- Case study and statistical study for TEC analysis
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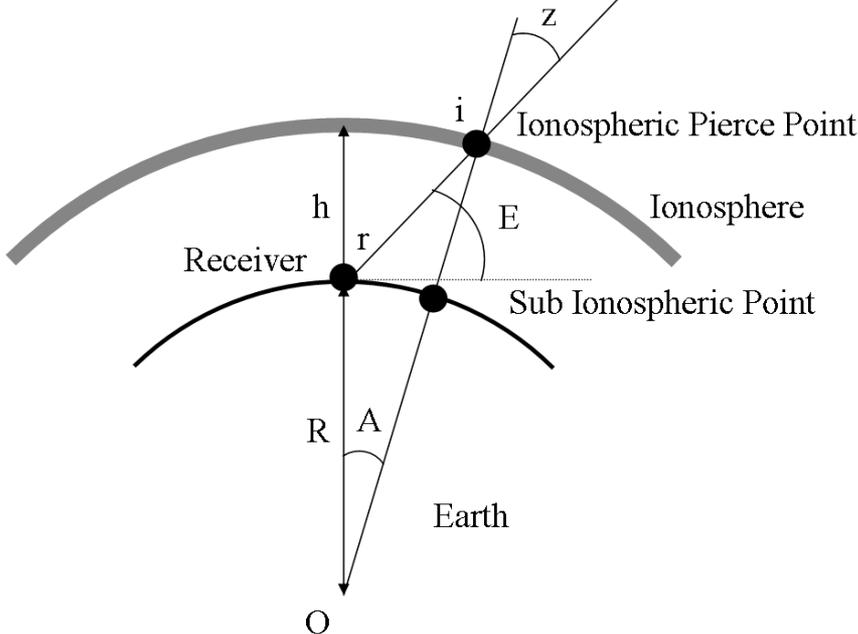
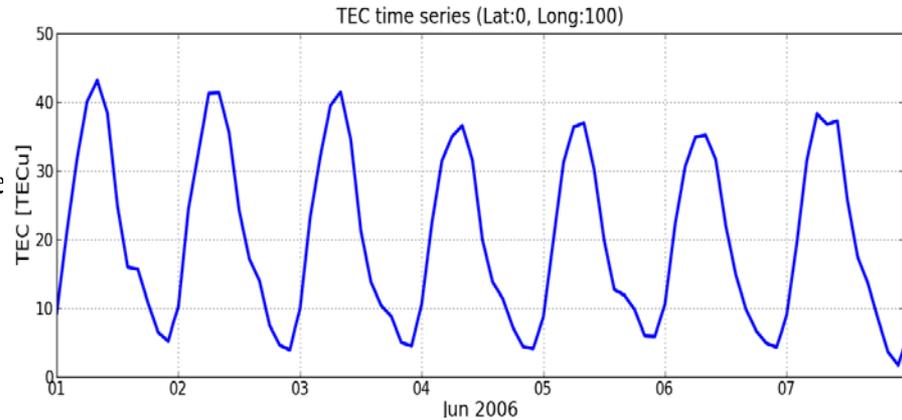
# Introduction

## How to identify Ionospheric anomalies

### Dual frequency

- L1: 1575.42 MHz
- L2: 1227.60 MHz

Satellite



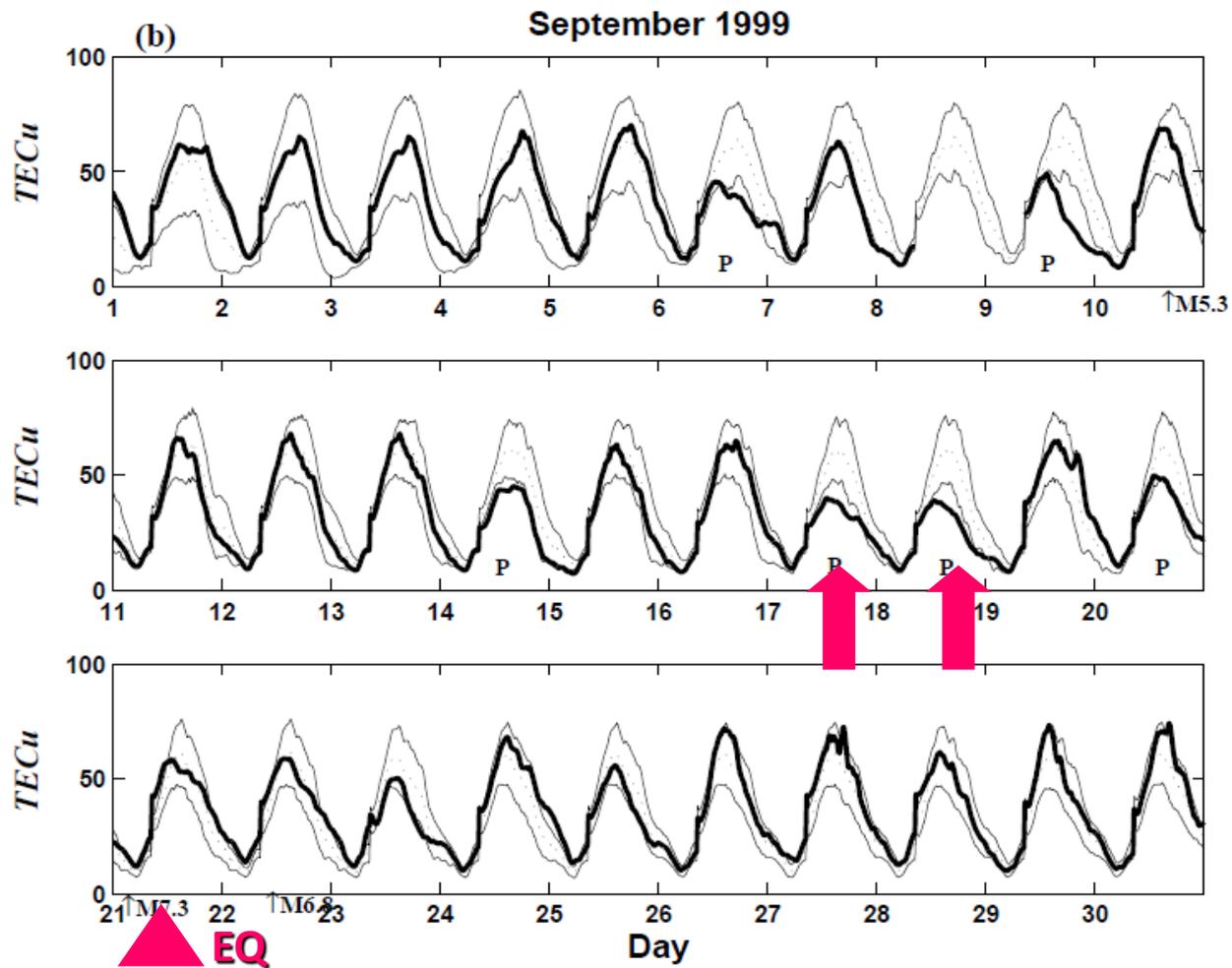
$$STEC = \frac{(f_{L1} f_{L2})^2}{40.3(f_{L1}^2 - f_{L2}^2)} (S_{L1} - S_{L2})$$

$$z = \arcsin \frac{R \cos E}{R + h}$$

$$VTEC = STEC \times \cos z$$

$$TEC : 1TECU : 10^{16} [el / m^2]$$

h= 3 5 0 km , R= 6 3 7  
0 km

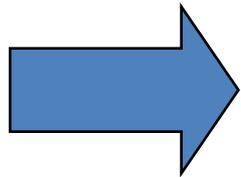


Taiwan ChiChi EQ

(Liu et al, 2000, 2001, 2004)

# Computation of TEC\* & GIM-TEC\*

To remove daily variation of TEC  
and identify abnormal signals associated with EQs



We computed the **15 days backward mean values**,  
and the associated standard deviation ( $\sigma$ )  
as a reference at specific times.

Then, we derived the normalized  $\Delta$ TEC (TEC\*).

$$\text{TEC}^*(t) = \frac{\text{TEC}(t) - \overline{\text{TEC}(t)}}{\sigma(t)}$$

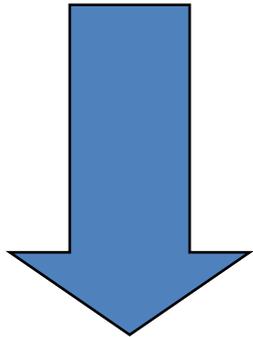
(computed using RINEX files)

$$\text{GIM-TEC}^*(t) = \frac{\text{GIM-TEC}(t) - \overline{\text{GIM-TEC}(t)}}{\sigma(t)}$$

# Removal of geomagnetic storm effect

To remove geomagnetic storm effect,  
we define a criterion as follows;

Dst index  $< -60$  nT : geomagnetic storm

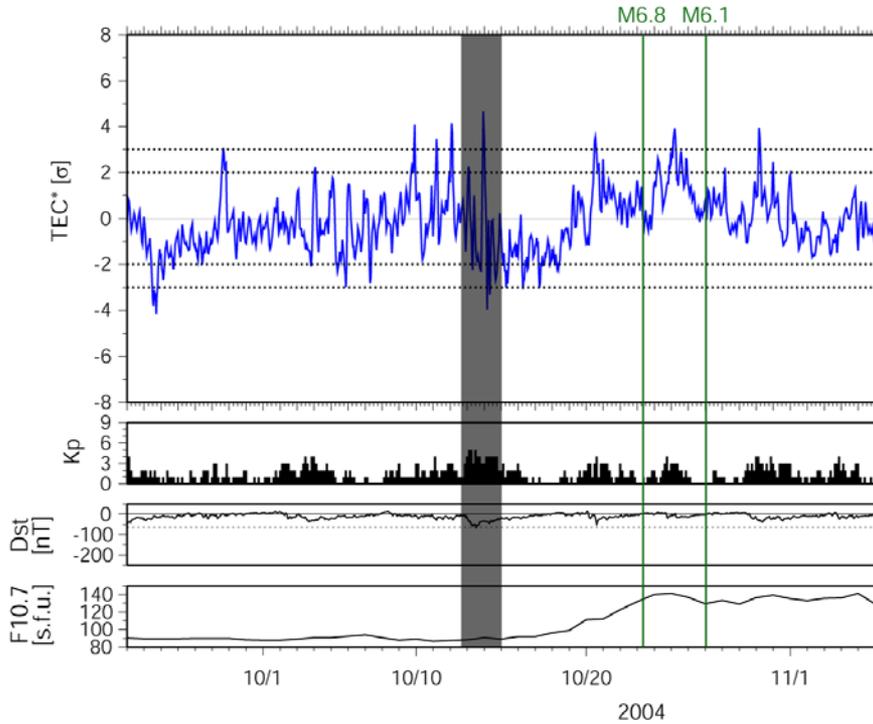


TEC could depress about a few hours  
to 2 days after geomagnetic storm onsets.  
(Kelley, 1989; Davies, 1990)

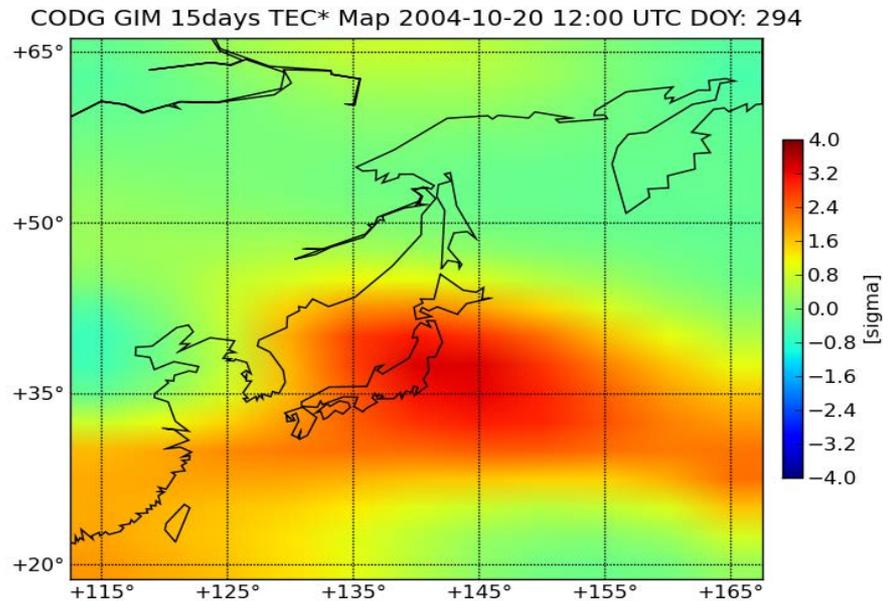
We removed the TEC data of geomagnetic  
storm period for 2 days after storm onset.

# Case study for the 20041023 Chuetsu EQ(M6.8) (Kon et al., JAES 2011)

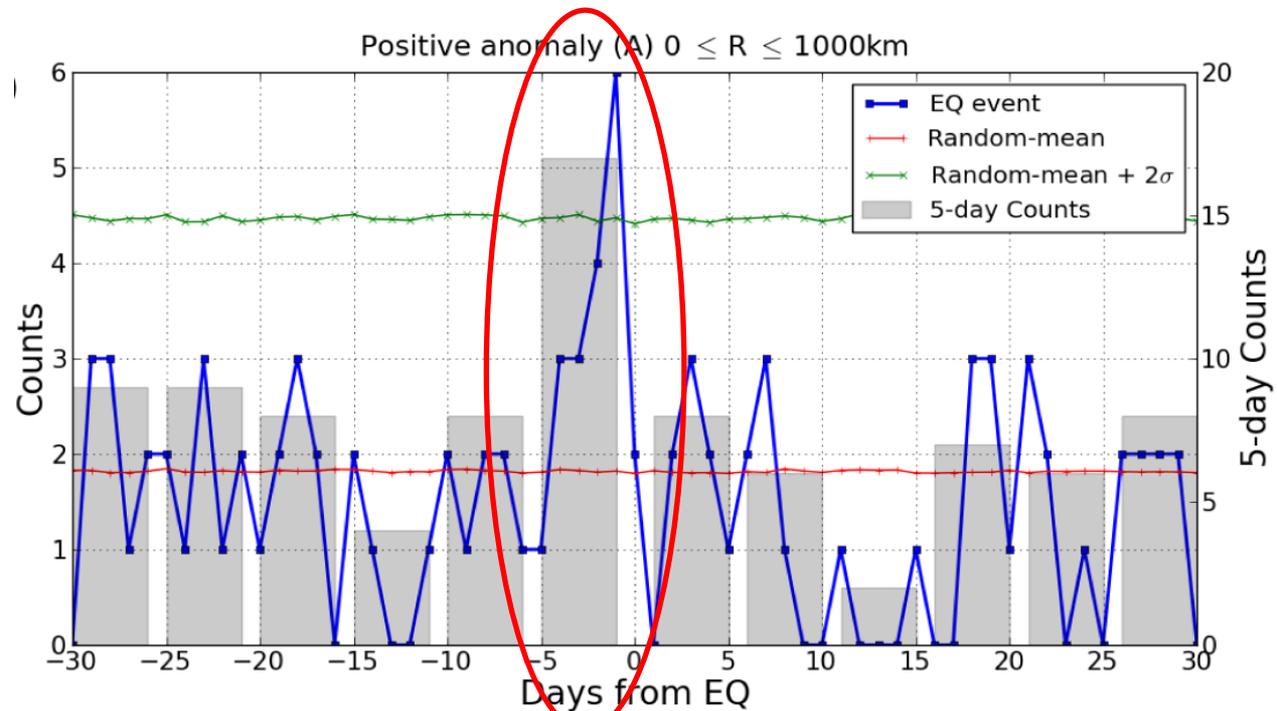
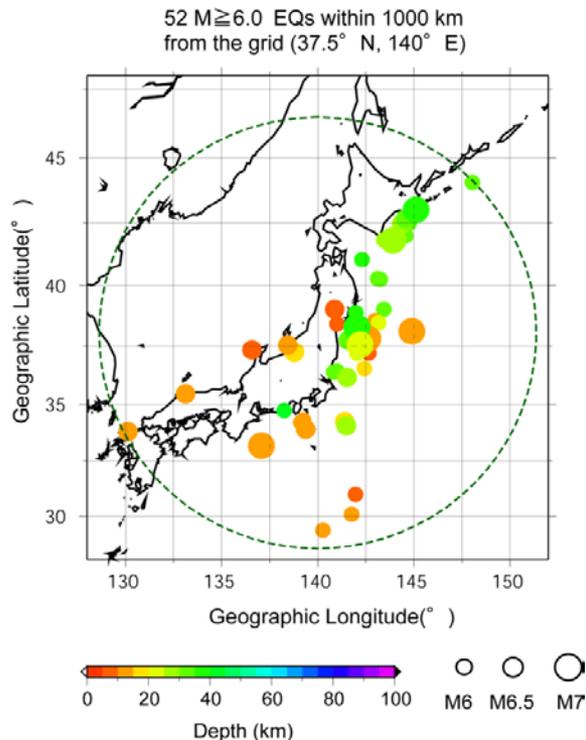
The 2004 mid-Niigata Prefecture Earthquake



Spatial Distribution of  
anomalous TEC



## Statistical Approach for 2D analysis

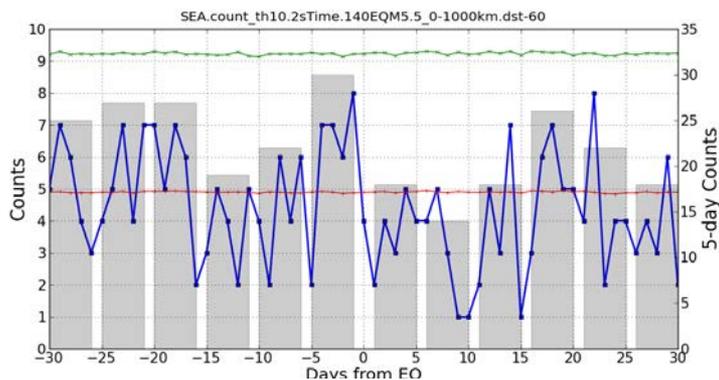


*Kon et al., 2011*

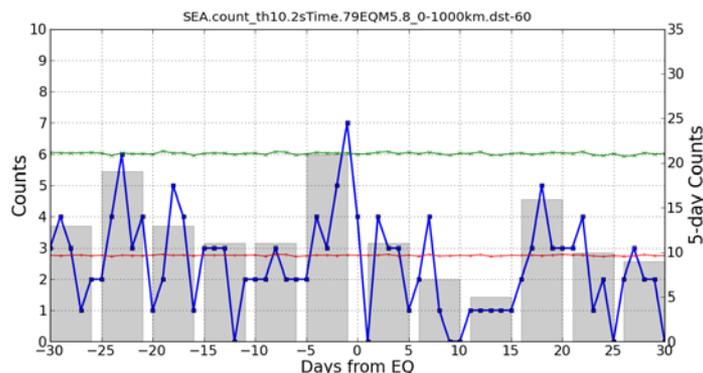


**Kon et al., 2011 shows that the Positive TEC anomaly with duration > 10 hours 1-5 days before EQs with  $M > 6$  and  $D < 40\text{km}$  is significant over Japan in 1998-2010 with magnitude and distance dependences**

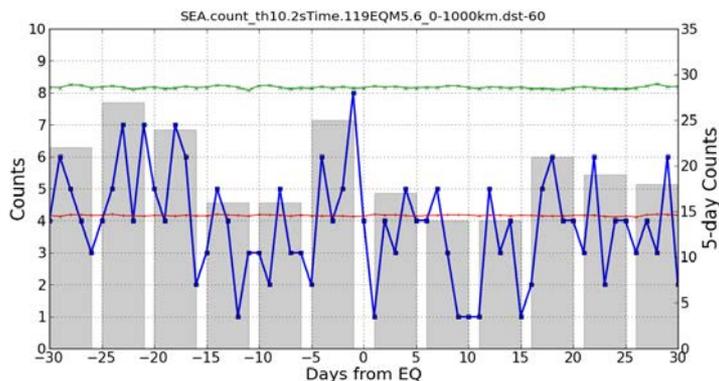
# Statistical Investigation of GPS-TEC anomaly over 1998-2010 (Superposed Epoch Analysis Normalized GIM-TEC\*) **Epidemiological approach**



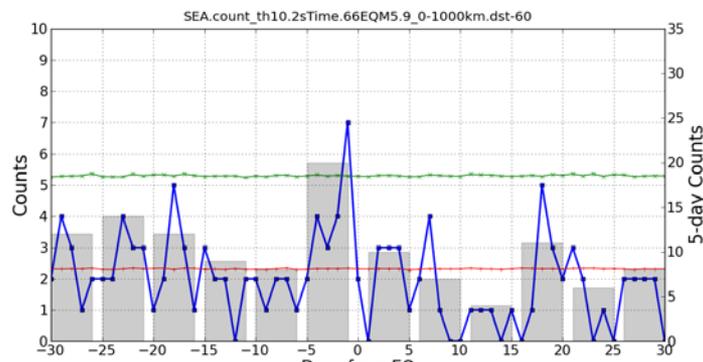
M>5.5  
140 EQs



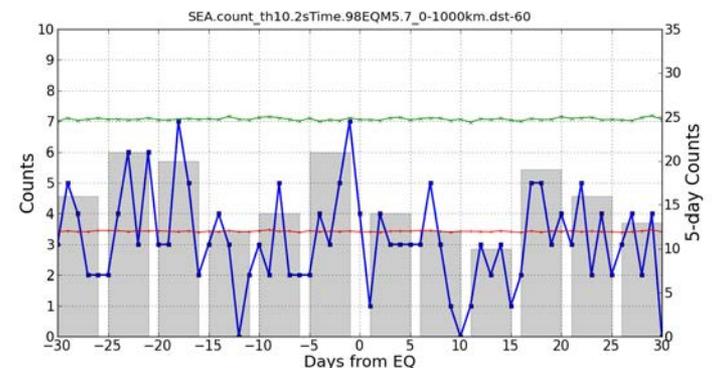
M>5.8  
79 EQs



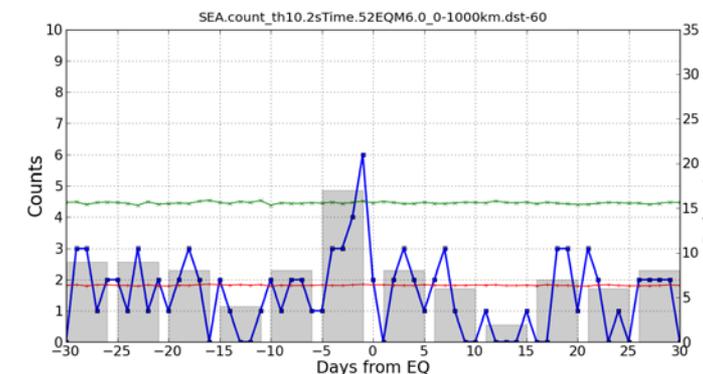
M>5.6  
119 EQs



M>5.9  
66 EQs



M>5.7  
98 EQs



M>6.0  
52 Eqs

(Kon et al  
2011)

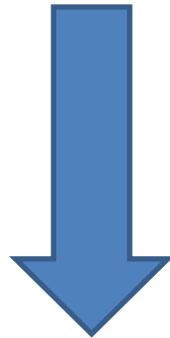
**Definition of Anomaly: Positive, Intensity  $>2\sigma$ , Duration  $>10$  hours/day**

# Removal of TEC anomaly related to magnetic storm

## Removal of geomagnetic effects in Kon et al., 2011

- Definition of magnetic storm :  $Dst < -60$  nT

Remove 2 days data after onset of the storm



From a few hours to 2 days after the onset of the magnetic storm, TEC decreases in lower and mid latitudes. (Kelley, 1989; Davies, 1990)

Evaluate the duration of ionospheric disturbance due to geomagnetic storm statistically, based on the observed data.

# Geomagnetic Storms

## Definition of geomagnetic storm

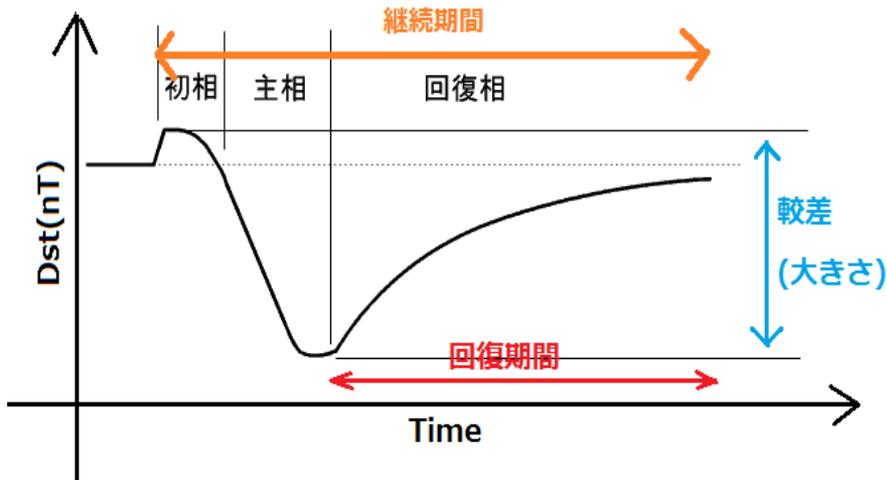
Dst index, WDC for Geomagnetism, Kyoto

Dst index (final report) (1998-2009)

Dst index (not final report) (2010-2012)

Dst index (first report) (2013)

Magnetic storm



Number of magnetic storm over 1998-2013

	Intensity (1) 60~79nT	Intensity (2) 80~99nT	Intensity (3) 100nT~	Total
Period 1 0000-0559LT	28	21	28	77
Period 2 0600-1159LT	31	22	27	80
Period 3 1200-1759LT	34	14	21	69
Period 4 1800-2359LT	25	15	28	68
<b>Total</b>	<b>118</b>	<b>72</b>	<b>104</b>	<b>294</b>

# Ionospheric perturbation after the onset of magnetic storm

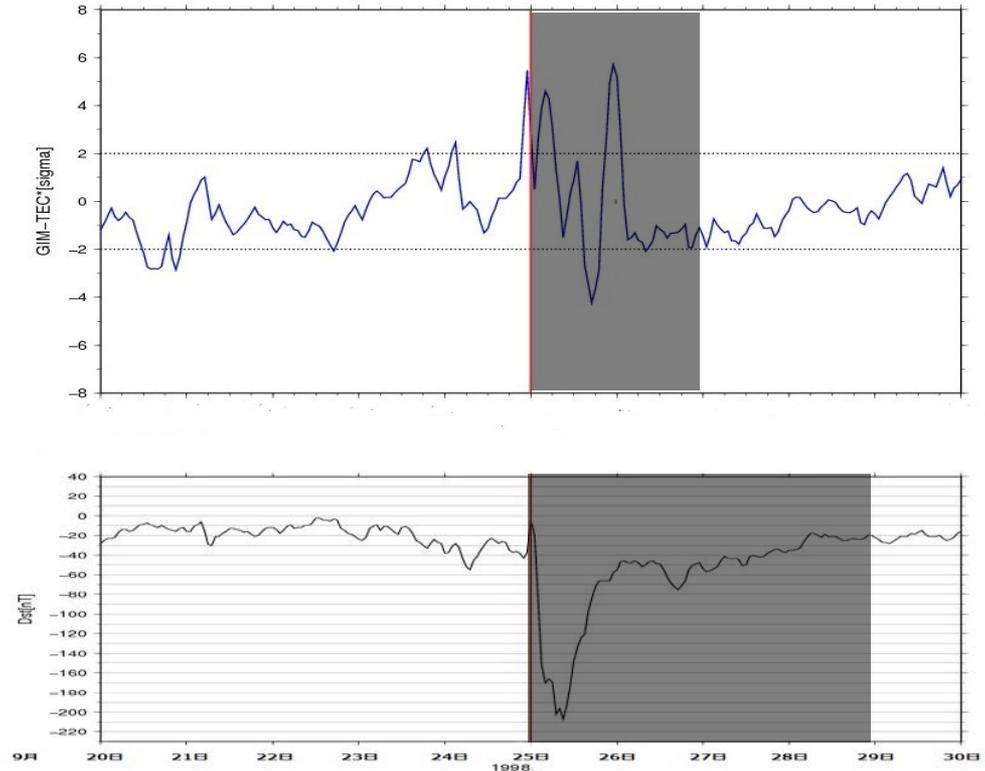
Geomagnetic storm and Ionospheric changes

## Ionospheric response of GIM-TEC\*

GIM-TEC\*

$$GIM-TEC^*(t) = \frac{TEC(t) - \overline{TEC(t)}}{\sigma(t)}$$

Definition of anomaly of GIM-TEC\*:  $\pm 2\sigma$



Geomagnetic storm at 0:00 on September 25, 1998 (UT)  
Storm class Intensity (3) and Period 1

# Statistical Analysis for Ionospheric variations

## Reduction of geomagnetic storm effects

### 【Procedure】

Extract -2 and +5 days GIM-TEC\* data after the onset of the magnetic storm for each class of the storm.

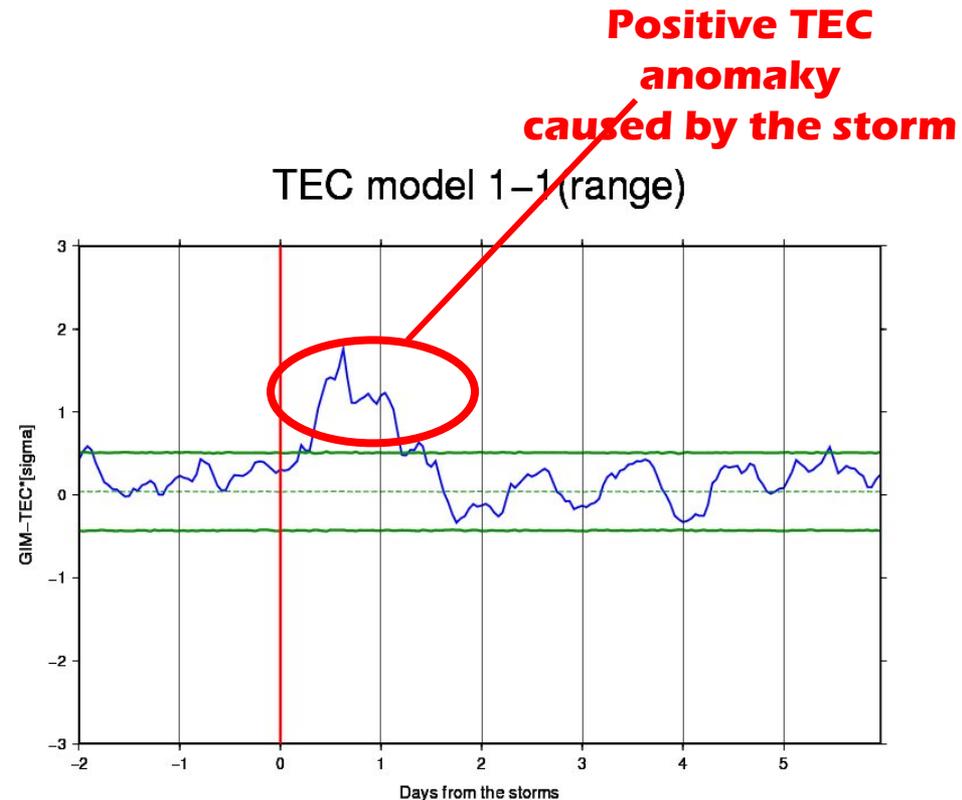


Apply the bootstrap method to increase number of data and take average.

Compute range of normal variation of GIM-TEC\*.



Determine the removal period of data due to geomagnetic storms for each group.



GIM-TEC\* variation model derived by statistical  
Computation for period 1 and intensity 1

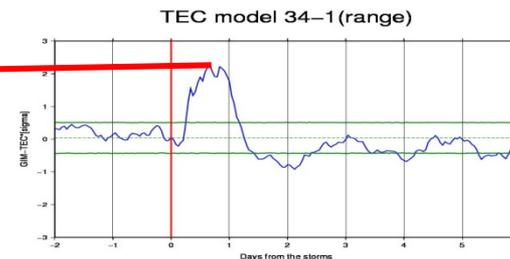
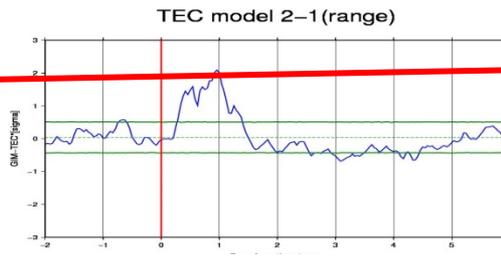
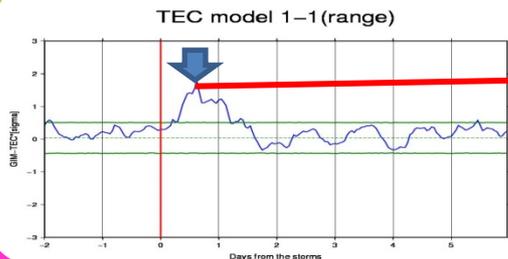
# Statistical models of ionospheric responses caused by geomagnetic storms

Intensity (1) (60-79nT)

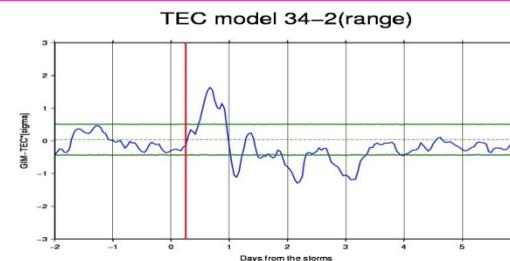
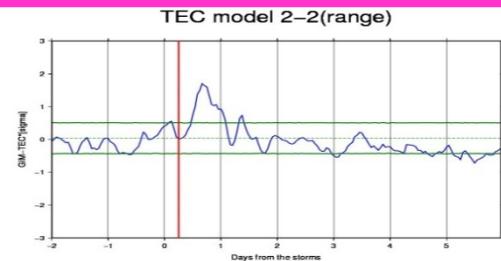
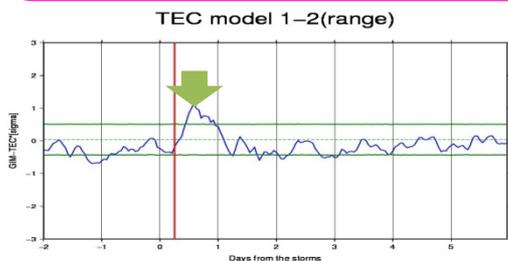
Intensity (2) (80-99nT)

Intensity (3) (100nT-)

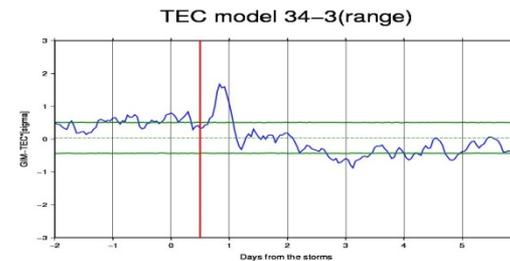
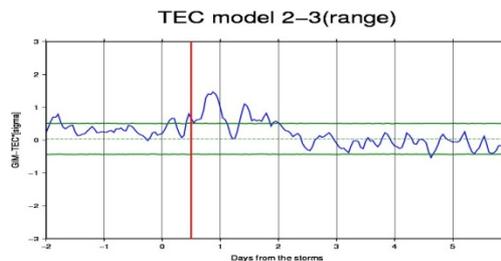
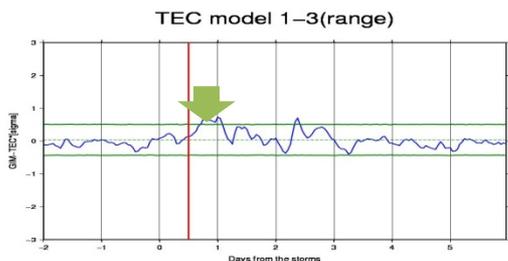
Period 1  
0000-0559LT



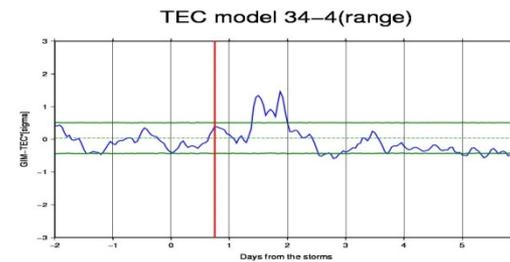
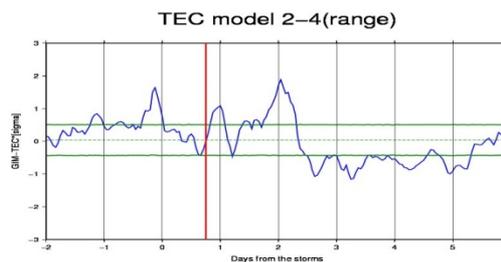
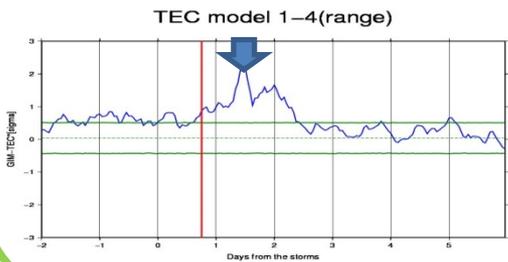
Period 2  
0600-1159LT



Period 3  
1200-1759LT



Period 4  
1800-2359LT



# Summary of Ionospheric responses

- Dependence of intensity of storm in that of Ionospheric perturbation
- For the onset time of period 4(1800-2359LT), there is a tendency that a positive anomaly seems to last so long.
- Positive anomalies occur just after the onset of magnetic storm for daytime (Periods 2 & 3), and a few hours after for nighttime (Periods 1 & 4).

Duration of magnetic storm (boot strap)

	Intens. (1)	Intens.(2)	Intens.(3)
Per.1	3 days	4 days	4 days
Per.2	2 days	3 days	4 days
Per.3	3 days	3 days	4 days
Per.4	3 days	3 days	4 days

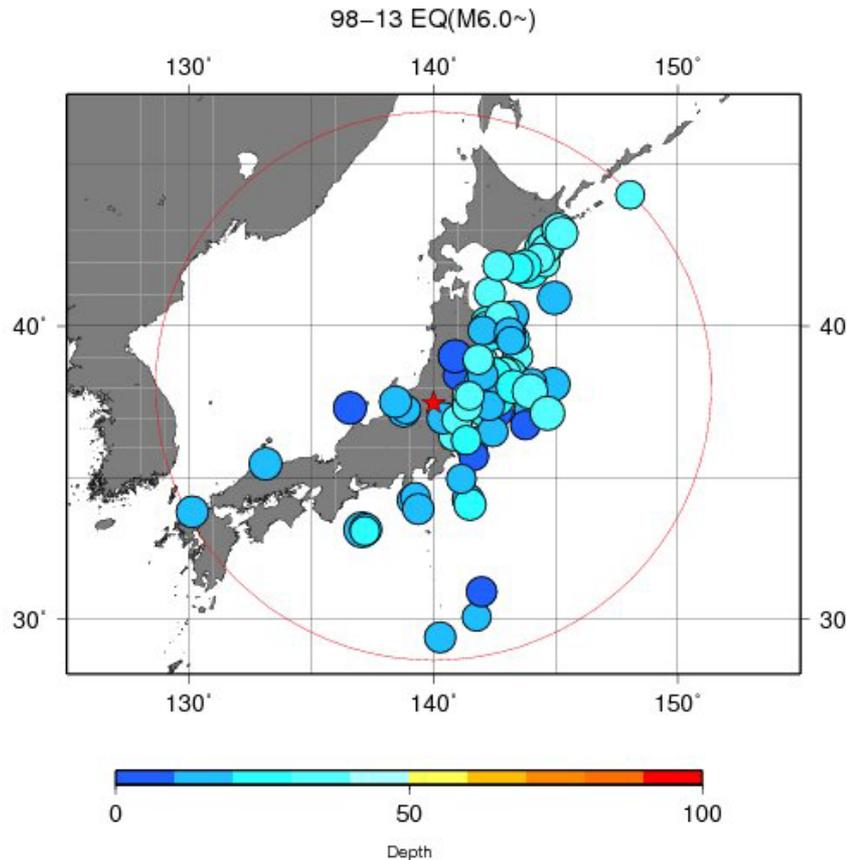
Appearance of positive anomalies

	Intens.(1)	Intens.(2)	Intens.(3)
Per.1	2 days	2 days	2 days
Per.2	1 day	2 days	1 day
Per.3	3 days	2 days	2 days
Per.4	5 days	3 days	3 days



Duration of magnetic storm and timing for appearance of positive anomalies is different.

# Significance check using Superposed Epoch Analysis (SEA) for 1998-2013



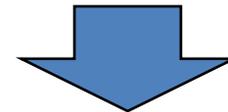
[EQ]

Period 1998/05 – 2013/12  
R < 1000km from (37.5° N,  
140° E)

$M \geq 6.0$ ,  $D \leq 40$  km

87 EQ

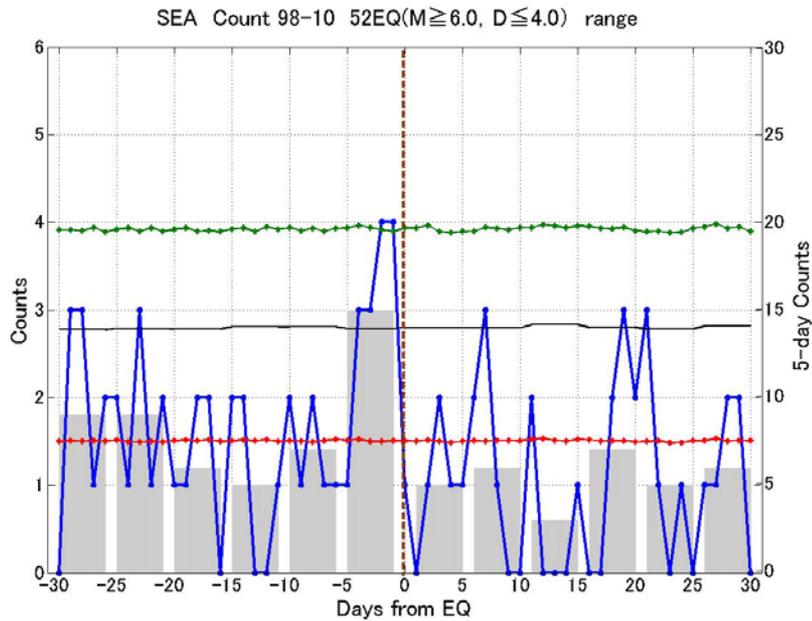
USGS EQ catalog



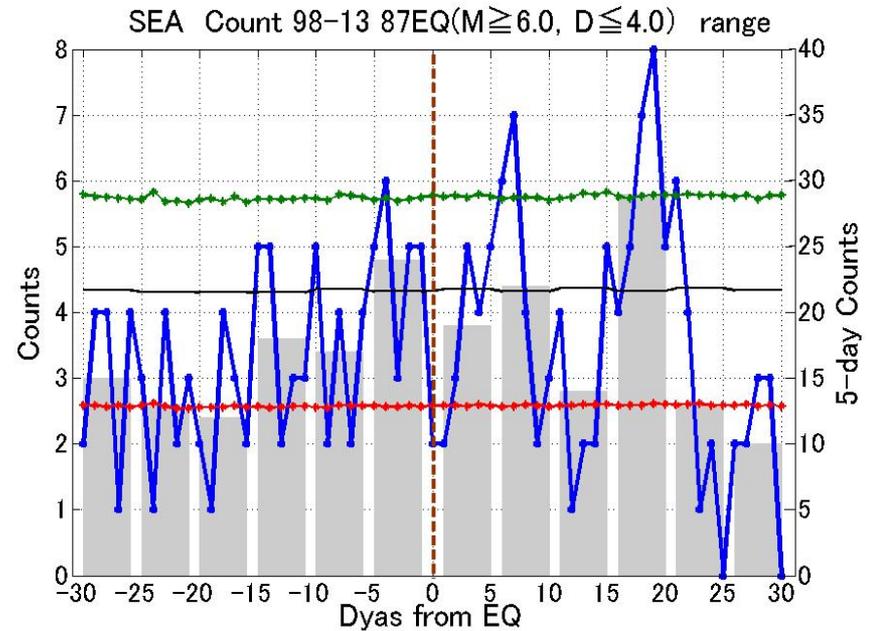
Superposed Epoch Analysis

# Results of SEA

52 EQ for 1998—2010

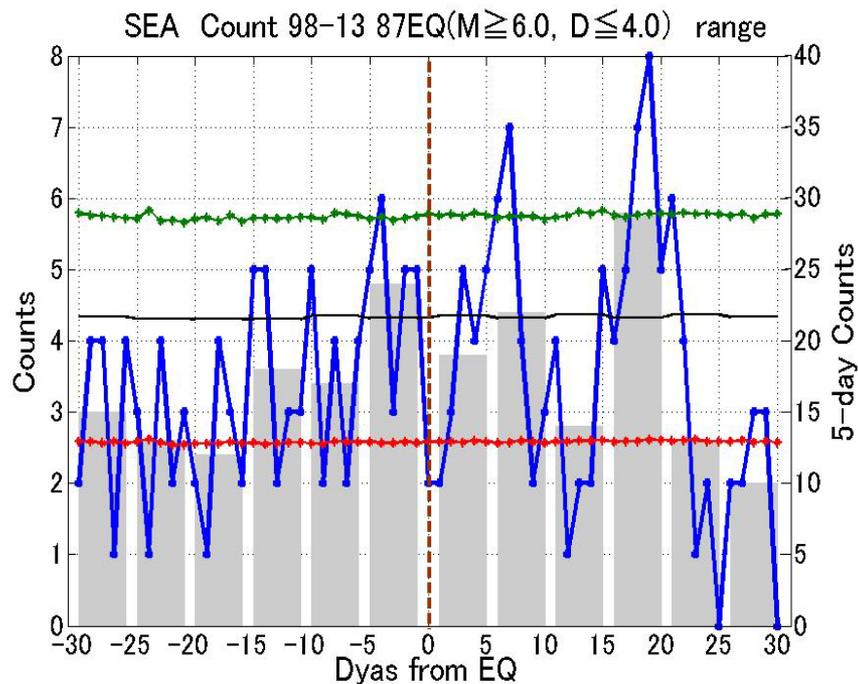


87 EQ during 1998-2013



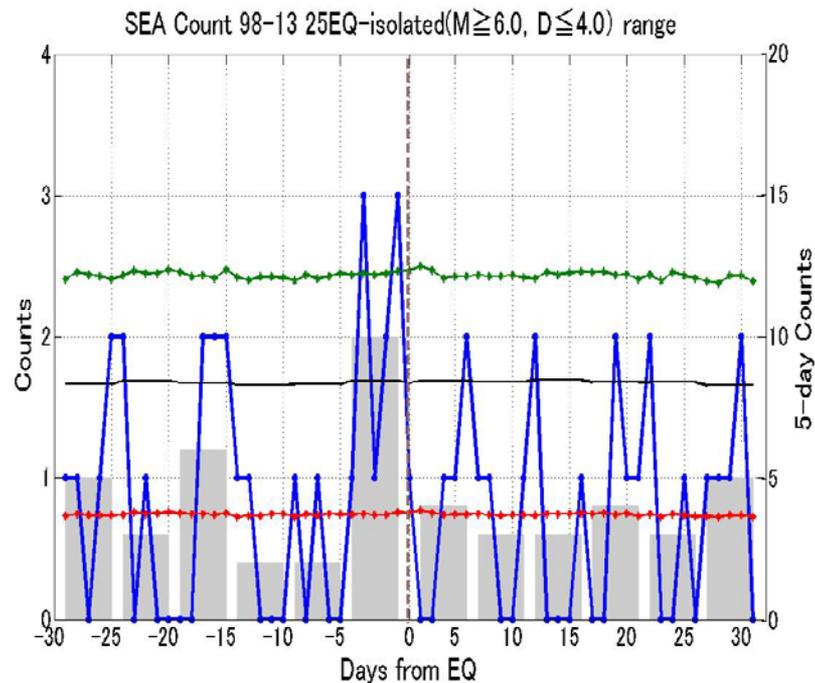
# SEA result remove EQs

Result for 87 EQ over 1998-2013.



Result for 25 isolated EQ s only over 1998-2013.

Isolated EQ; there are no EQ 30 days before and after the EQ.

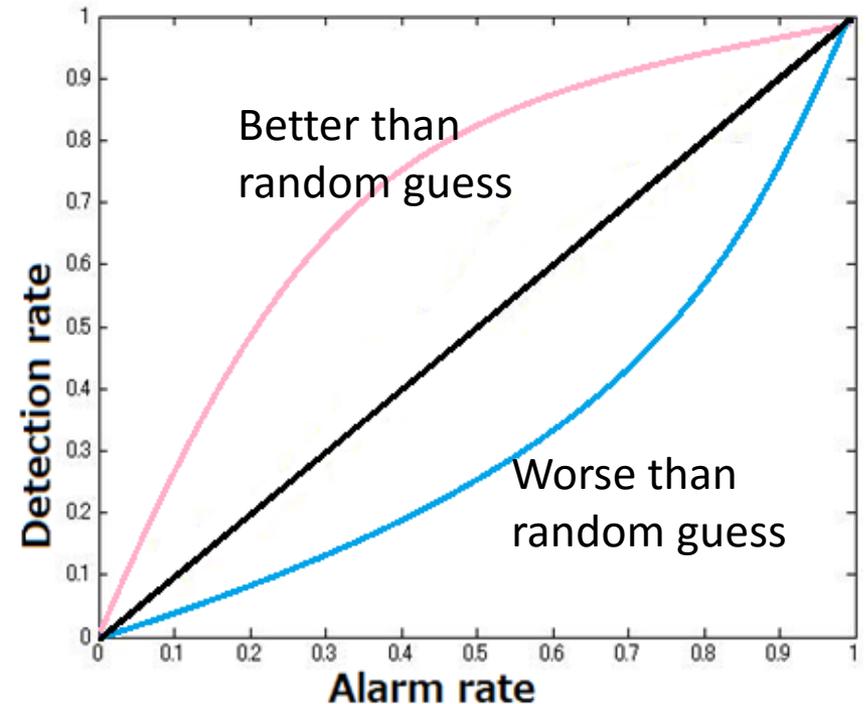


# Evaluation of efficiency of short-term forecast using Molchan's error diagram

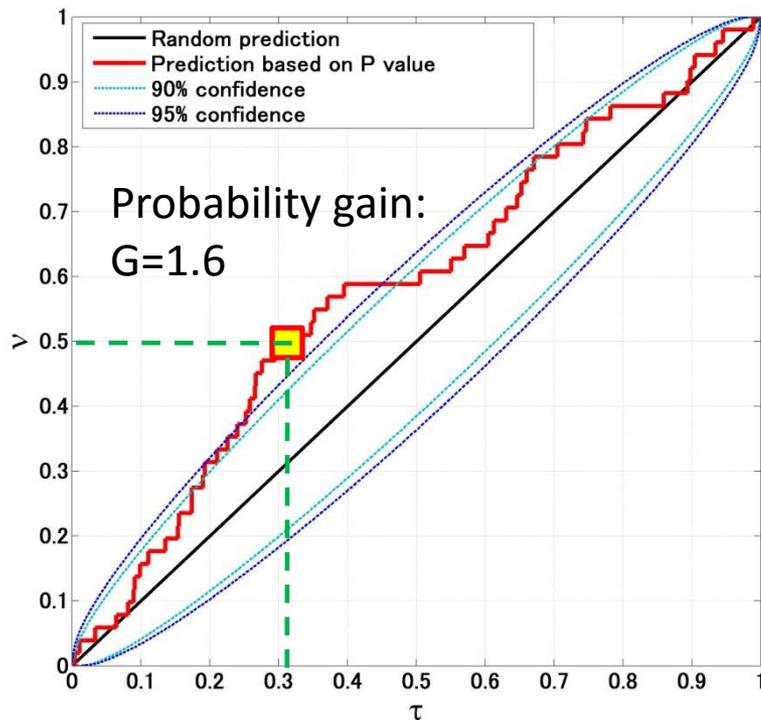
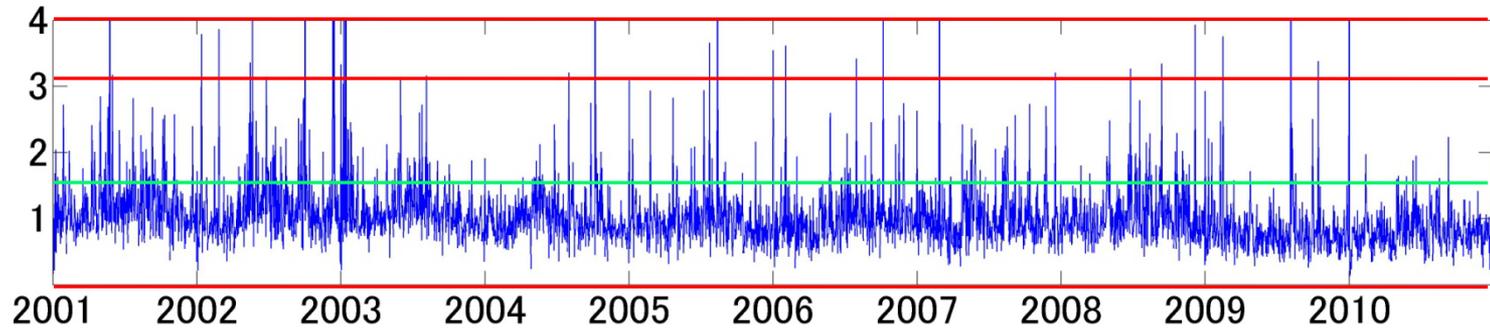
- a: the number of successful predictions of EQs
- b: the number of false alarms
- c: the number of successful predictions of non-occurrence
- d: the number of missed EQ

The proportion of predicted EQs,  
 $\nu = a / (a + d)$

The proportion of alarmed cells,  
 $\tau = (a + b) / (a + b + c + d)$



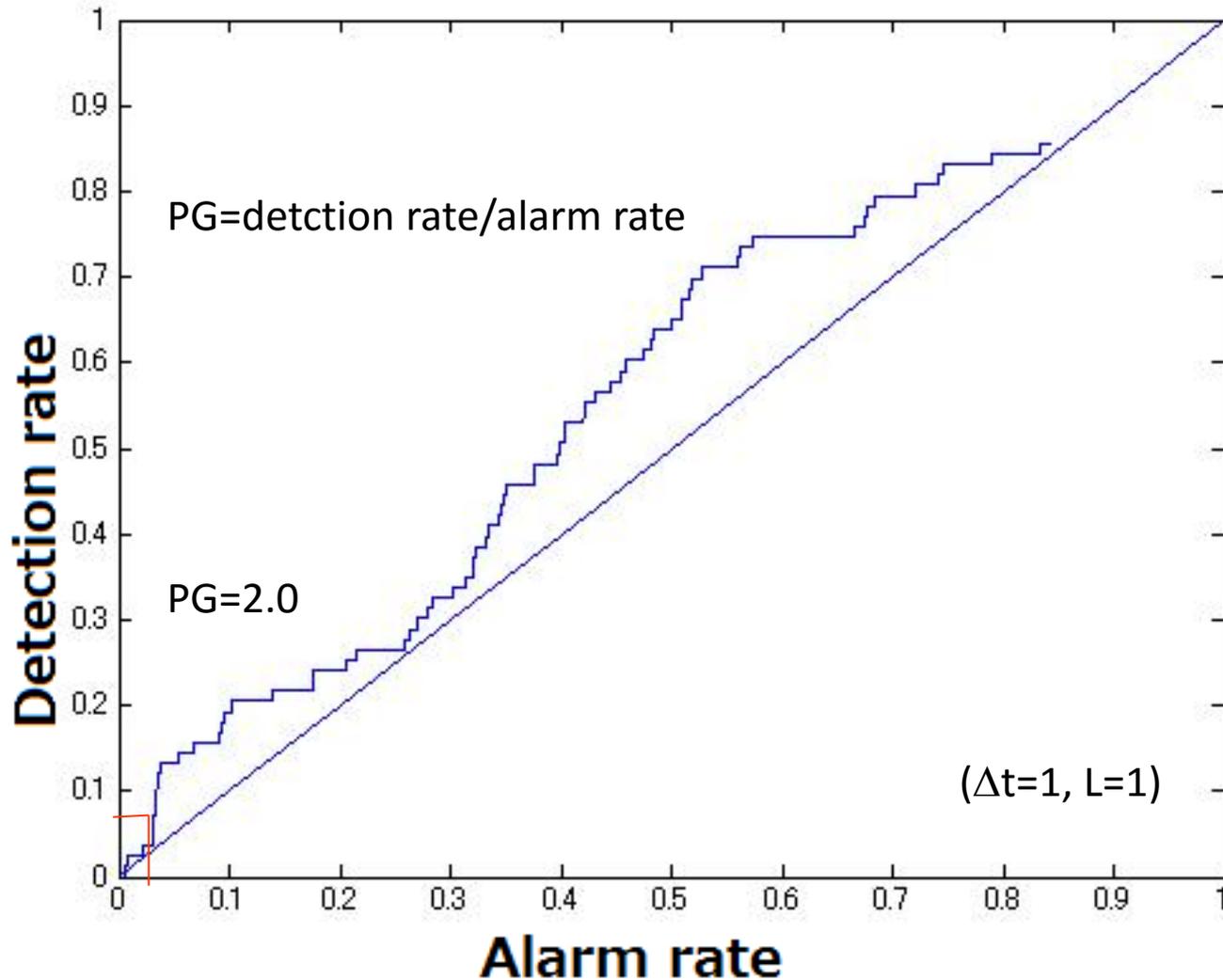
# Concept of the evaluation of the efficiency of ionospheric TEC phenomena for earthquake forecasting



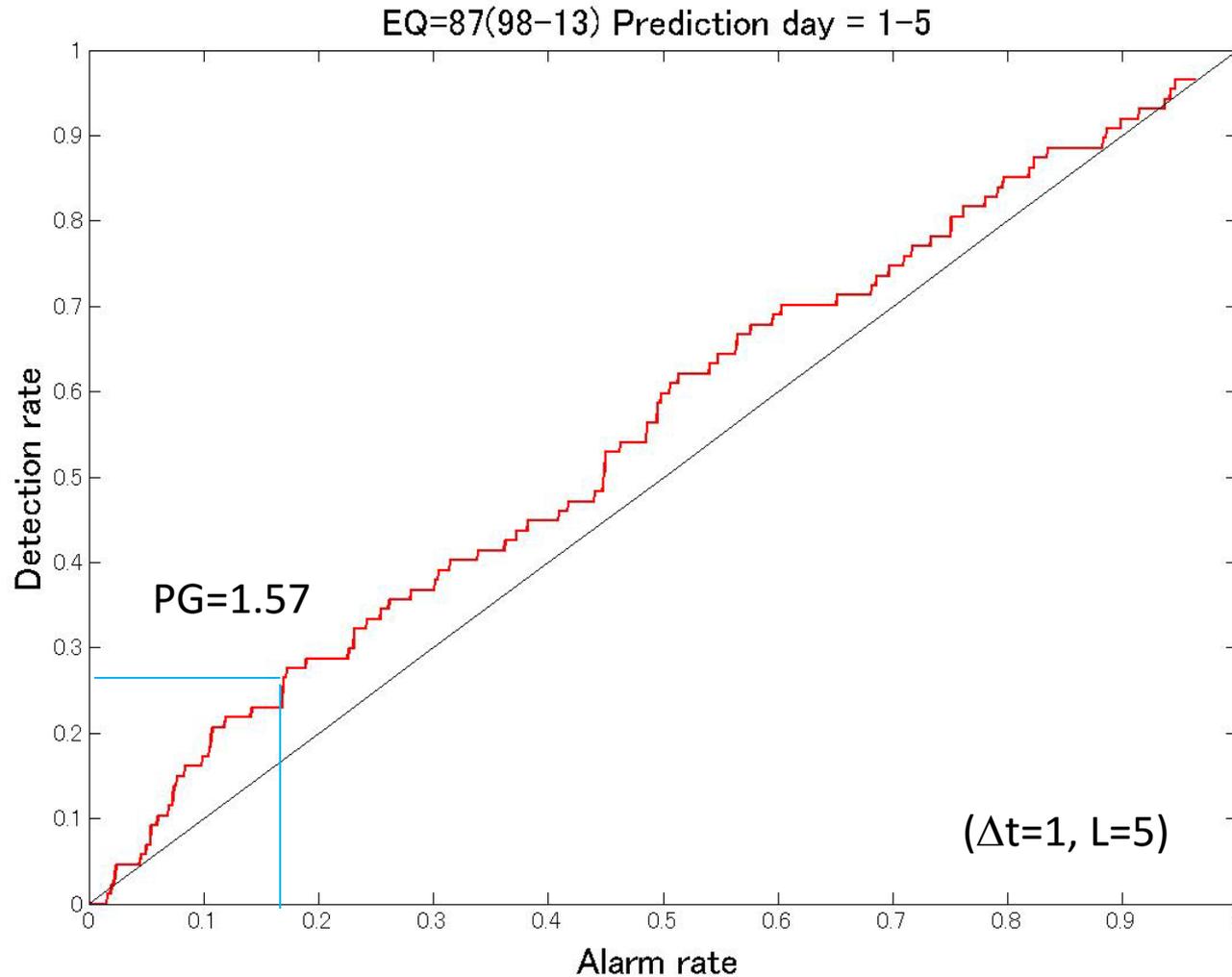
For example,  
 $\Delta$  (lead time) = 1 day  
L (alarm window) = 5 days  
and change threshold of the anomaly.

Molchan's error diagram for earthquake predictions using "anomalies in the Data set A" as precursors.

# Results of Molchans' Error Diagram Analysis during 1998-2013 (EQ $M \geq 6.0$ , $D \leq 40\text{km}$ )



# Result Molchan's Error Diagram



# Ionospheric Tomography using local GPS network (GEONET)

- Data

- 80 GPS stations
- 3 Ionosonde stations  
(NmF2, hmF2)

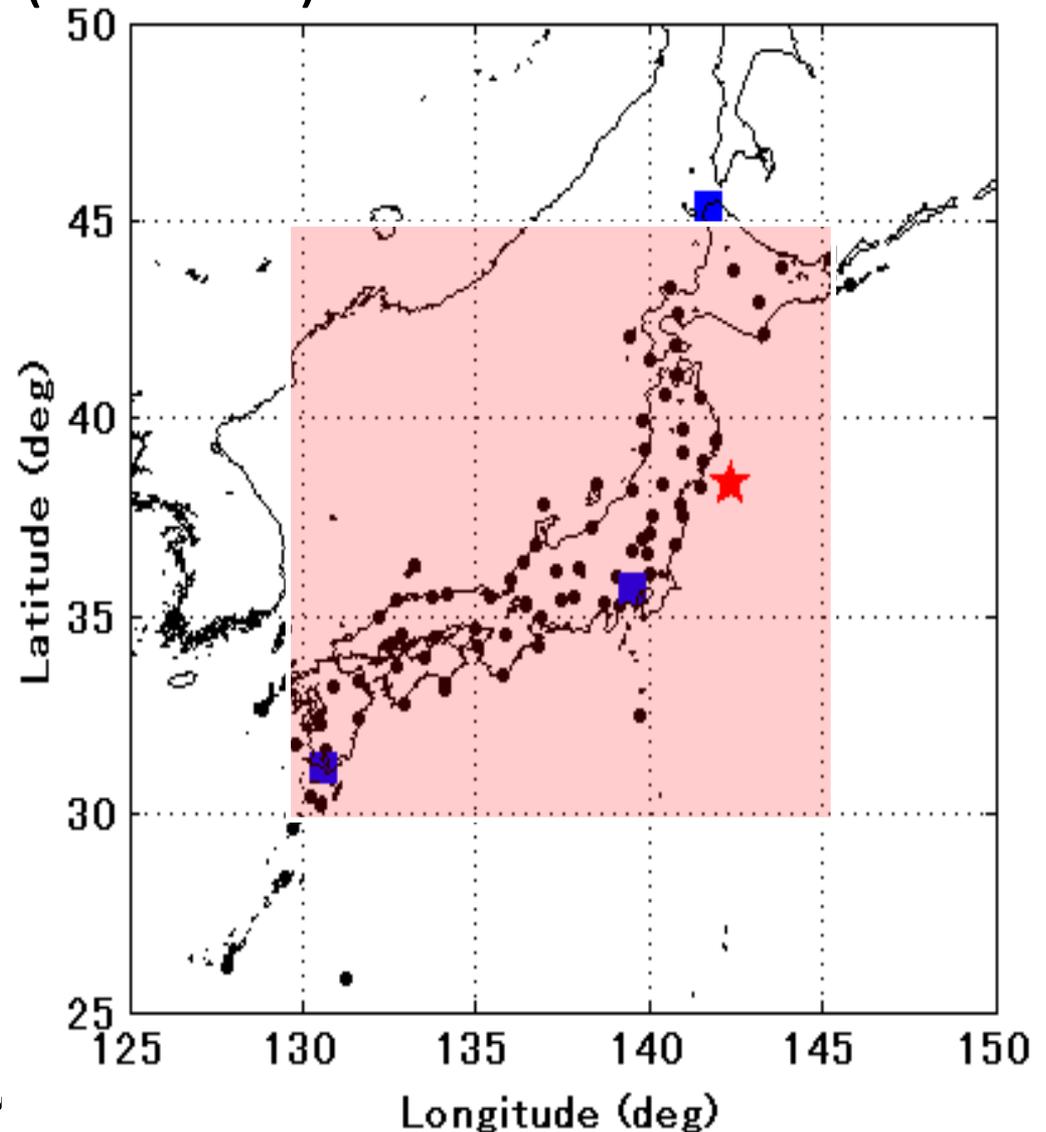
Wakkanai,  
Kokubunji,  
Yamakawa

- reconstructed area

Lat.  $30 - 45^{\circ}$  N,  
Long.  $130 - 145^{\circ}$  E  
height: 100 – 700 km

- spatial resolution :

$0.5^{\circ} \times 0.5^{\circ} \times 30$  km



(Hirooka et al., Radio Sci., 2011,  
Hirooka et al., NHESS, 2011)

# Residual Minimization Training Neural Network (RMTNN)

(Ma's approach (Ma et al., 2005))

Ionospheric Tomography

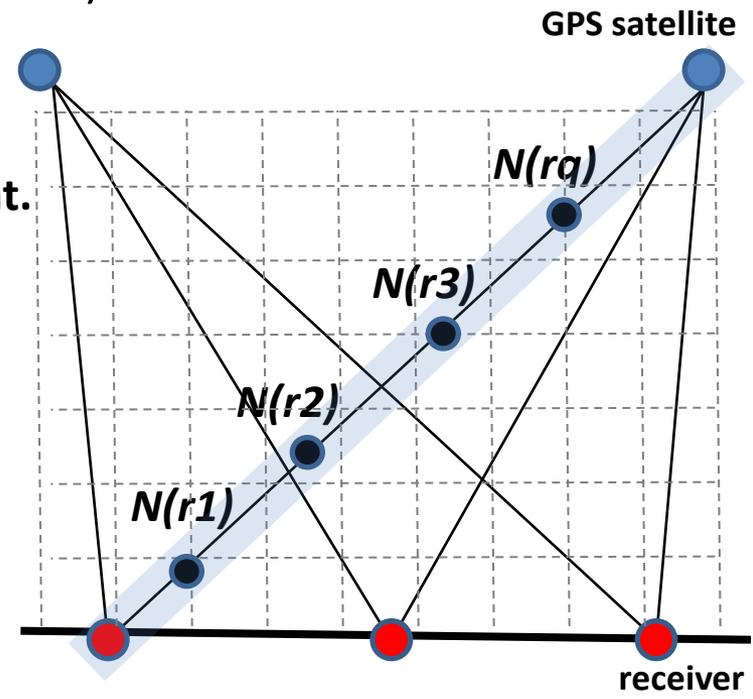
Observation : TEC along the line between rec. and sat.



No Info. for inputs (lat., long., alt.)



Minimize the residual of objective function



## ◆ Objective Function

$$E_{gps} = \sum_{p=1}^P \left( \sum_{q=1}^Q \alpha_q N(\vec{r}) + B_i + B_j + P_i^j - I_i^j \right)^2$$

$I_j^i = \text{SlantTEC}$   
 $B_i = \text{Bias of } i\text{th receiver}$   
 $B_j = \text{Bias of } j\text{th GPS satellite}$

$\alpha$  : weight  
 $P$  : TEC in plasmasphere

## NeQuick Model

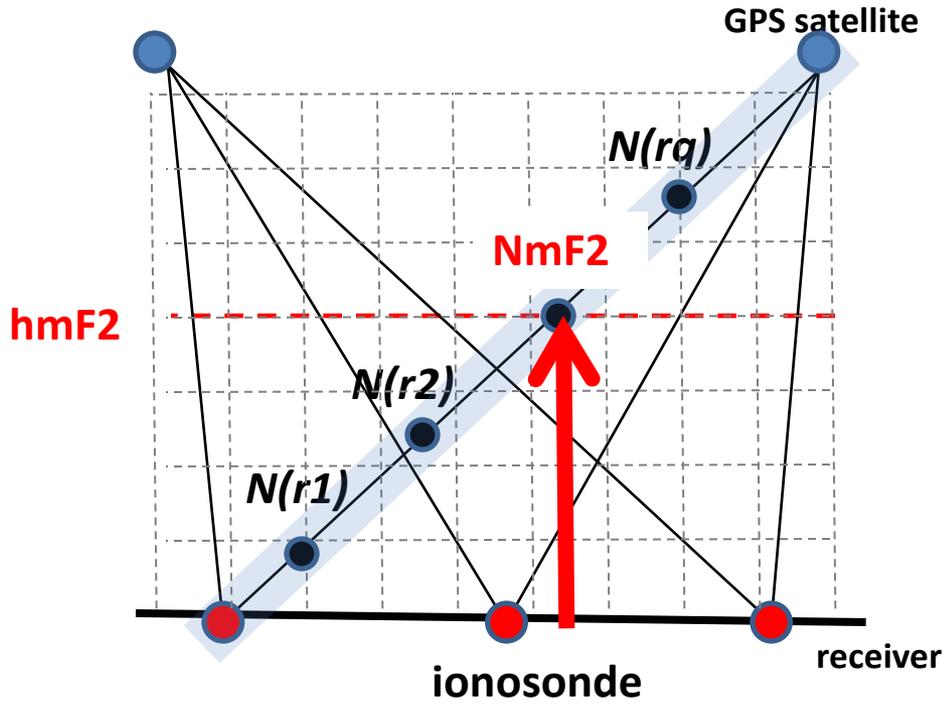
$$P_i^j \approx \frac{1}{\cos \theta} n_0 H_s$$

$n_0$  : ElectronDensity(700km)  
 $H_s$  : ScaleHeight(const)  
 $\theta$  : Zenith Angle

# Restriction for reconstruction

Lack of vertical information

Using Ionosonde data (density NmF2 and height hmF2) as a restriction



◆ cost function for Ionosonde data

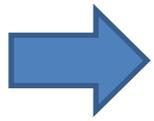
$$E_{ionosonde} = \sum_{s=1}^S (N_s - N_s^{ion})^2$$

$S$  : Number of Ionosonde

◆ cost function for system

$$E = gE_{gps} + E_{ionosonde}$$

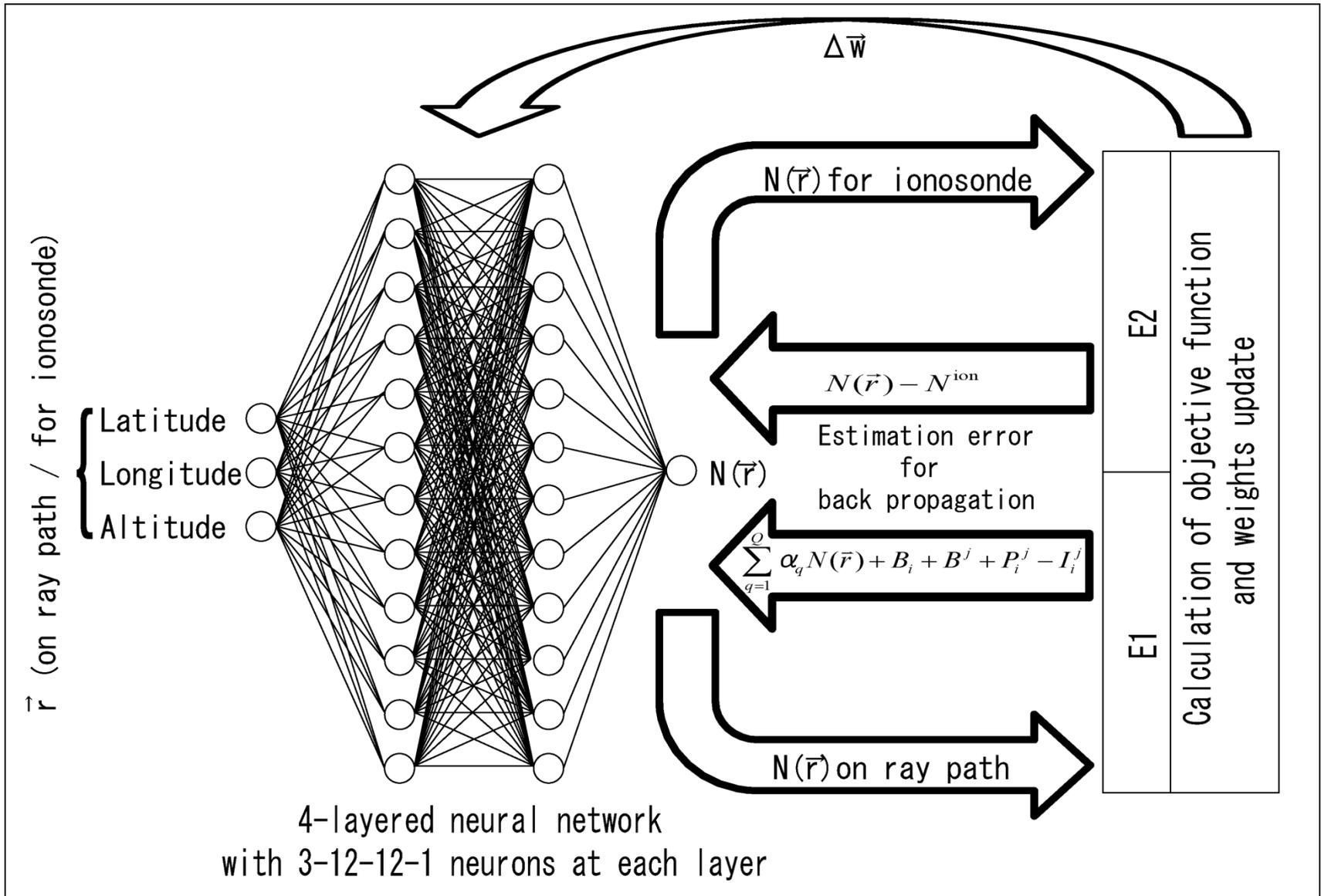
$g$  : Lagrange's coefficient



Supervise to minimize function E

Restriction of Ionosonde and other Data make improve reconstruction results.

# System design of NN based Ionospheric tomography

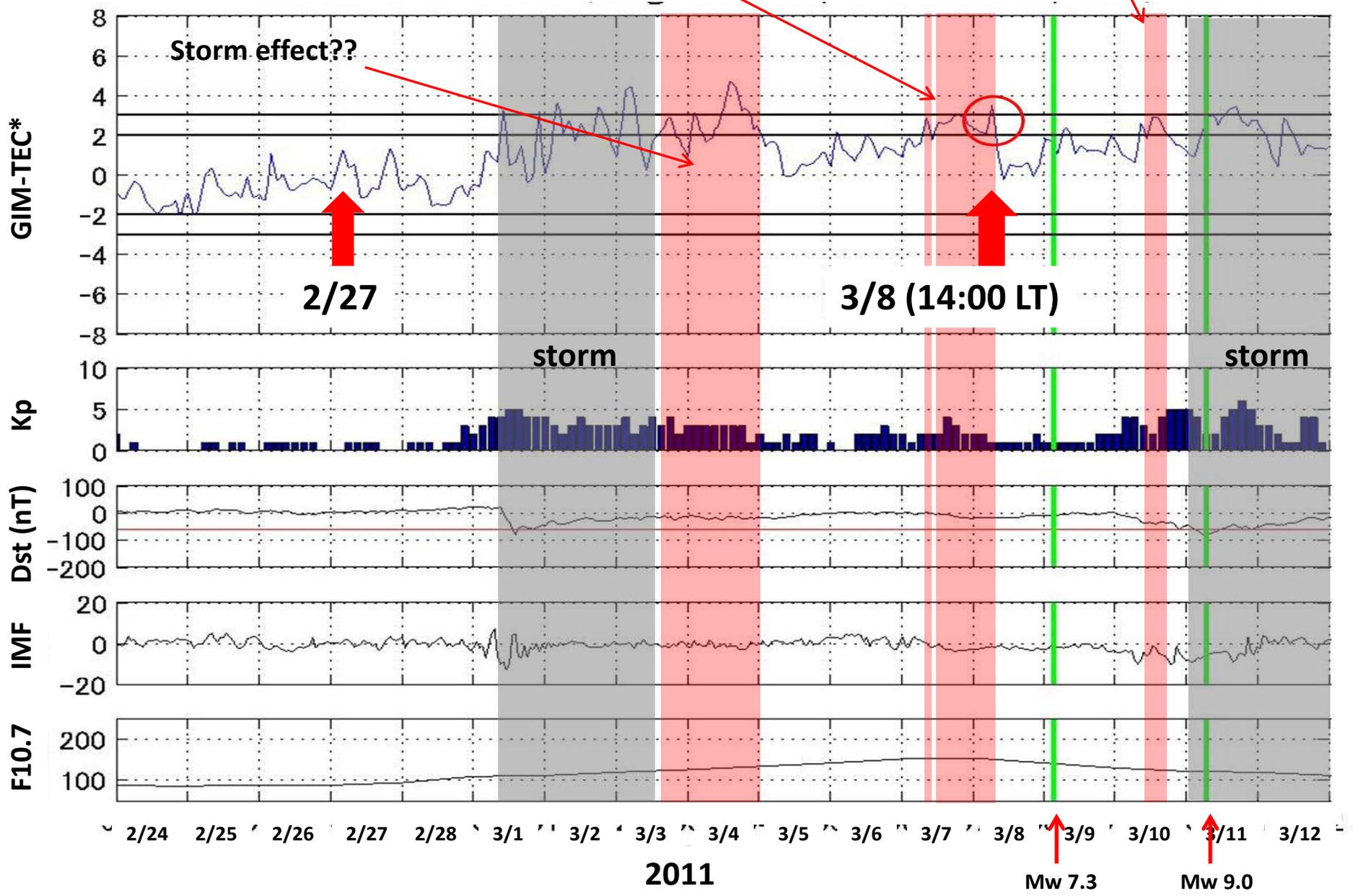


# GIM-TEC\* variation over Sendai area

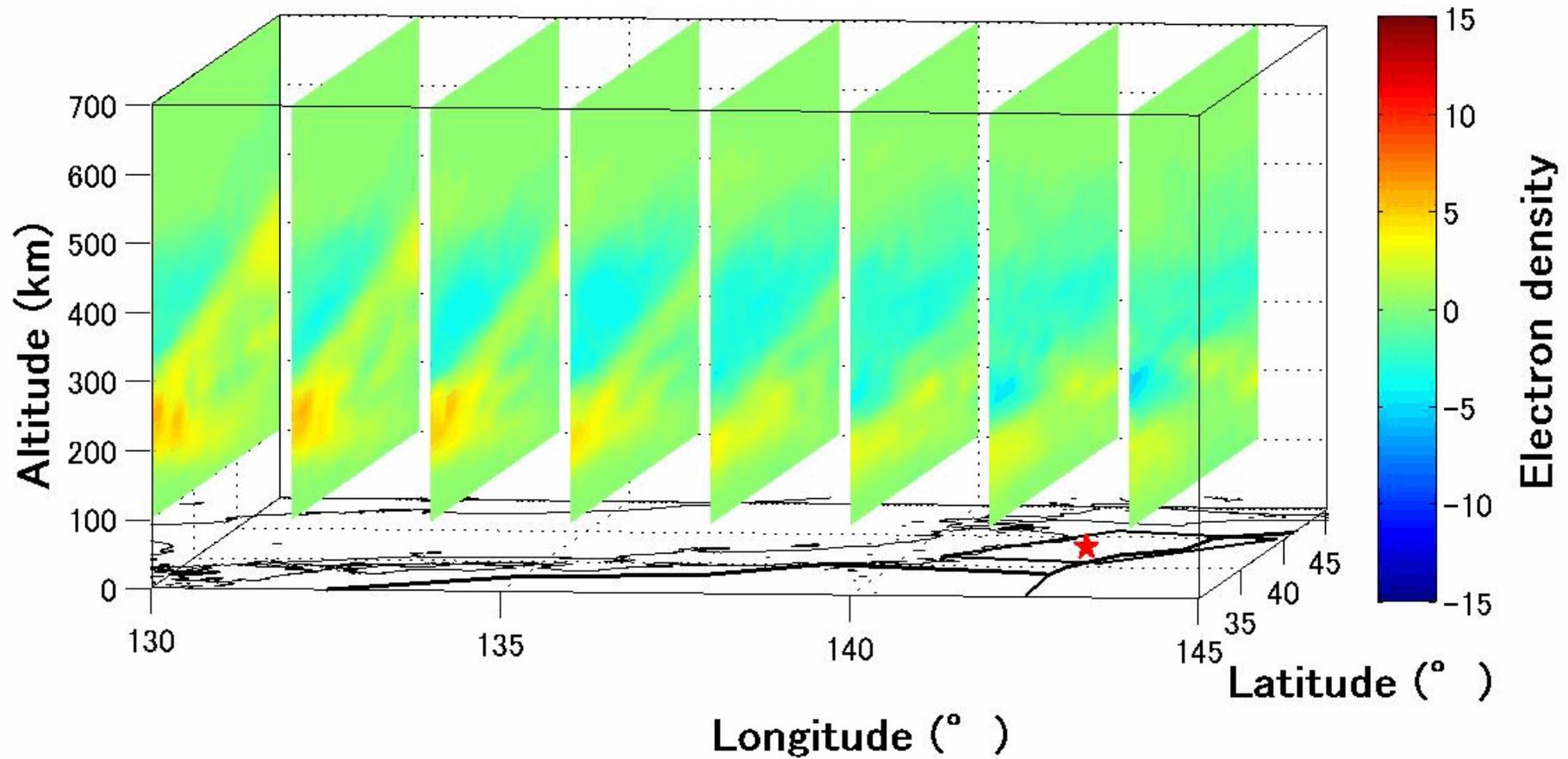
3/7:16-18 LT, 3/7:20 LT – 3/8:16 LT

3/10:17-18,20-24 LT

(20 hours duration)



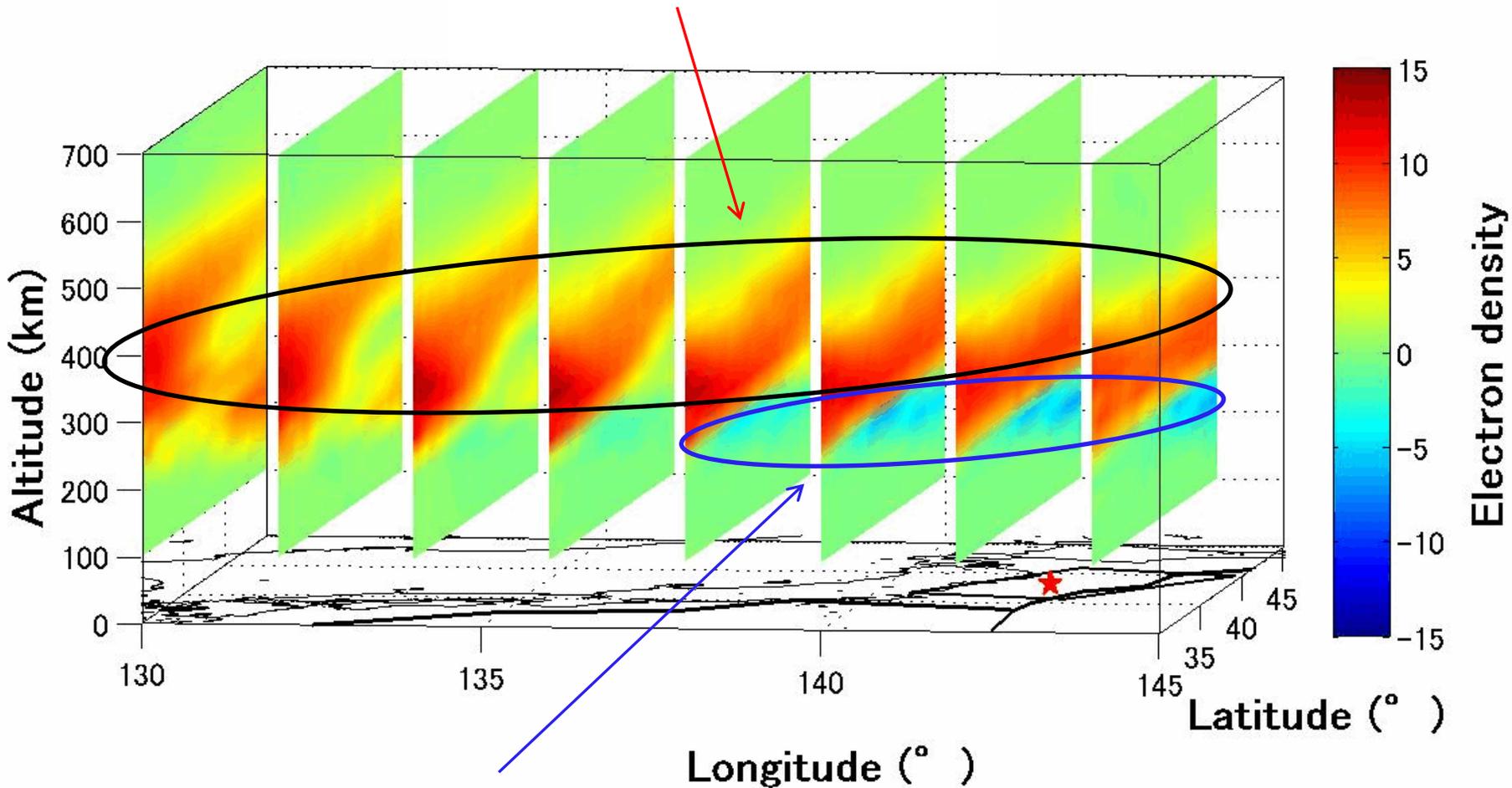
GIM-TEC\* : No anomaly (13:00 LT on Feb. 27)



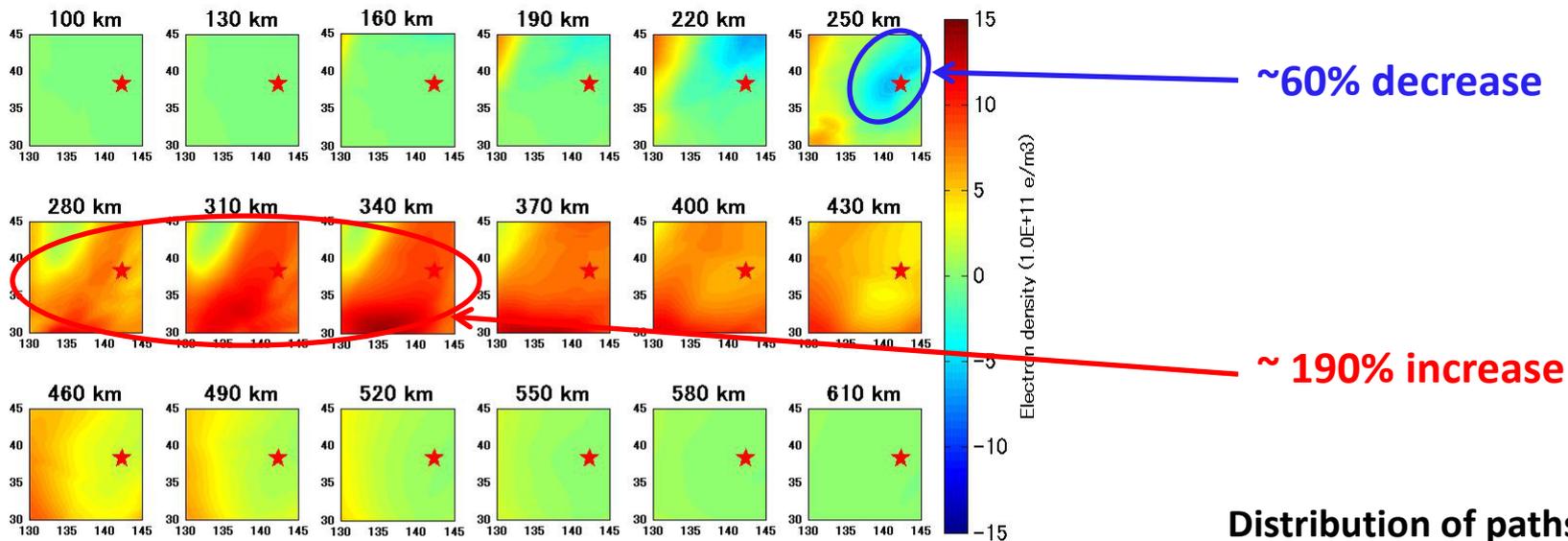
**GIM-TEC\* : Anomalous day  
(13:00 LT on March 8)**

**Differential Image**

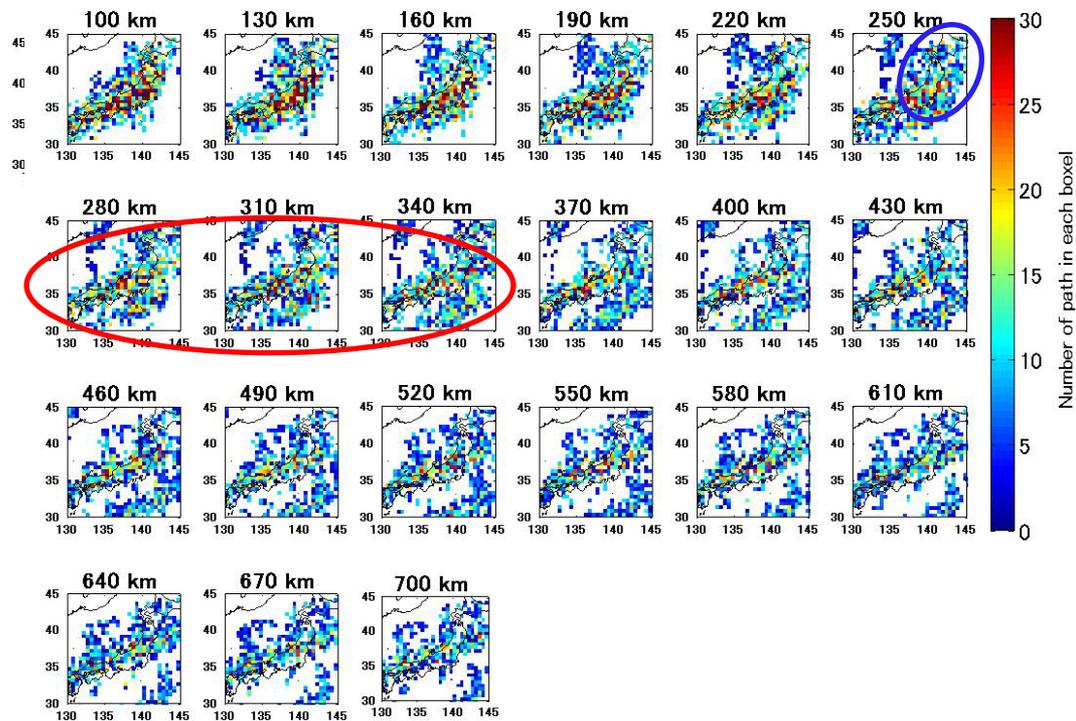
**Positive enhancement of electron density (+190%)**



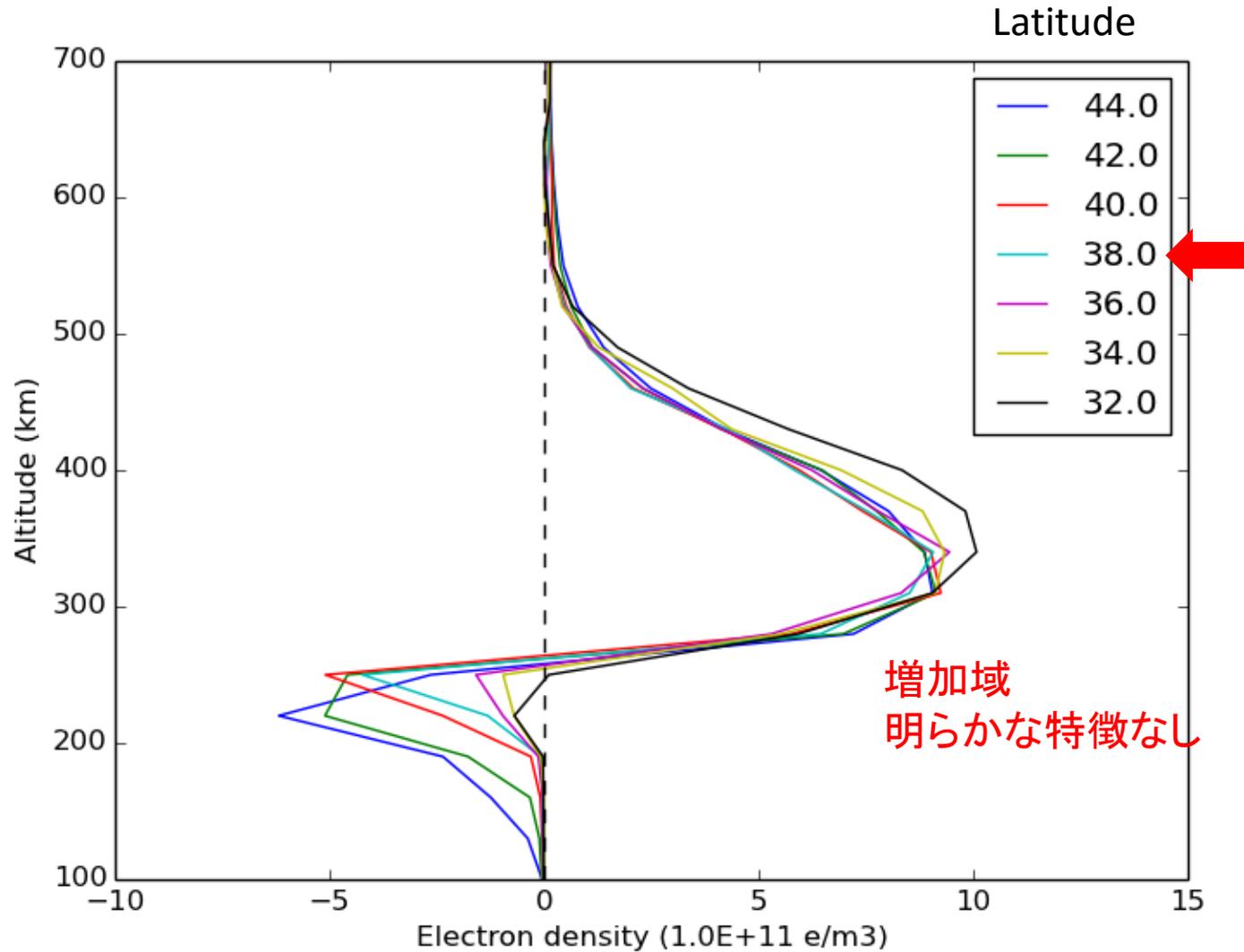
**local decrease of electron density over epicenter (~60%)**



### Distribution of paths



# Electron density profile at different latitudes for the 20110311 M9 EQ (differential values from 15 days backward median)

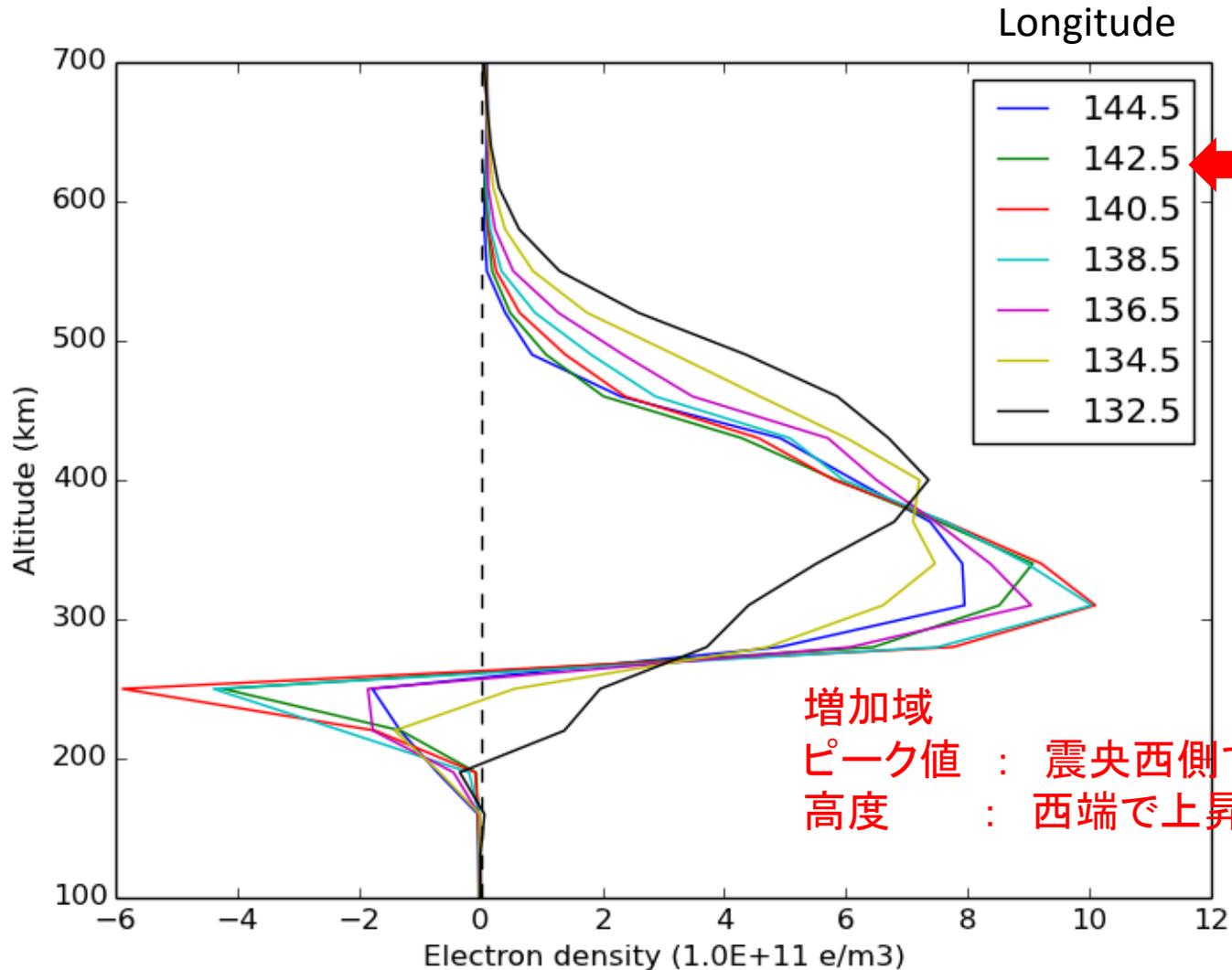


減少域

ピーク値 : 高緯度から低緯度へ徐々に低くなる

高度 : 震央付近で最も高くなる

# Electron density profile at different longitudes for the 20110311 M9 EQ (differential values from 15 days backward median)



減少域

ピーク値 : 震央付近で最も高くなる

高度 : 大きな変化なし



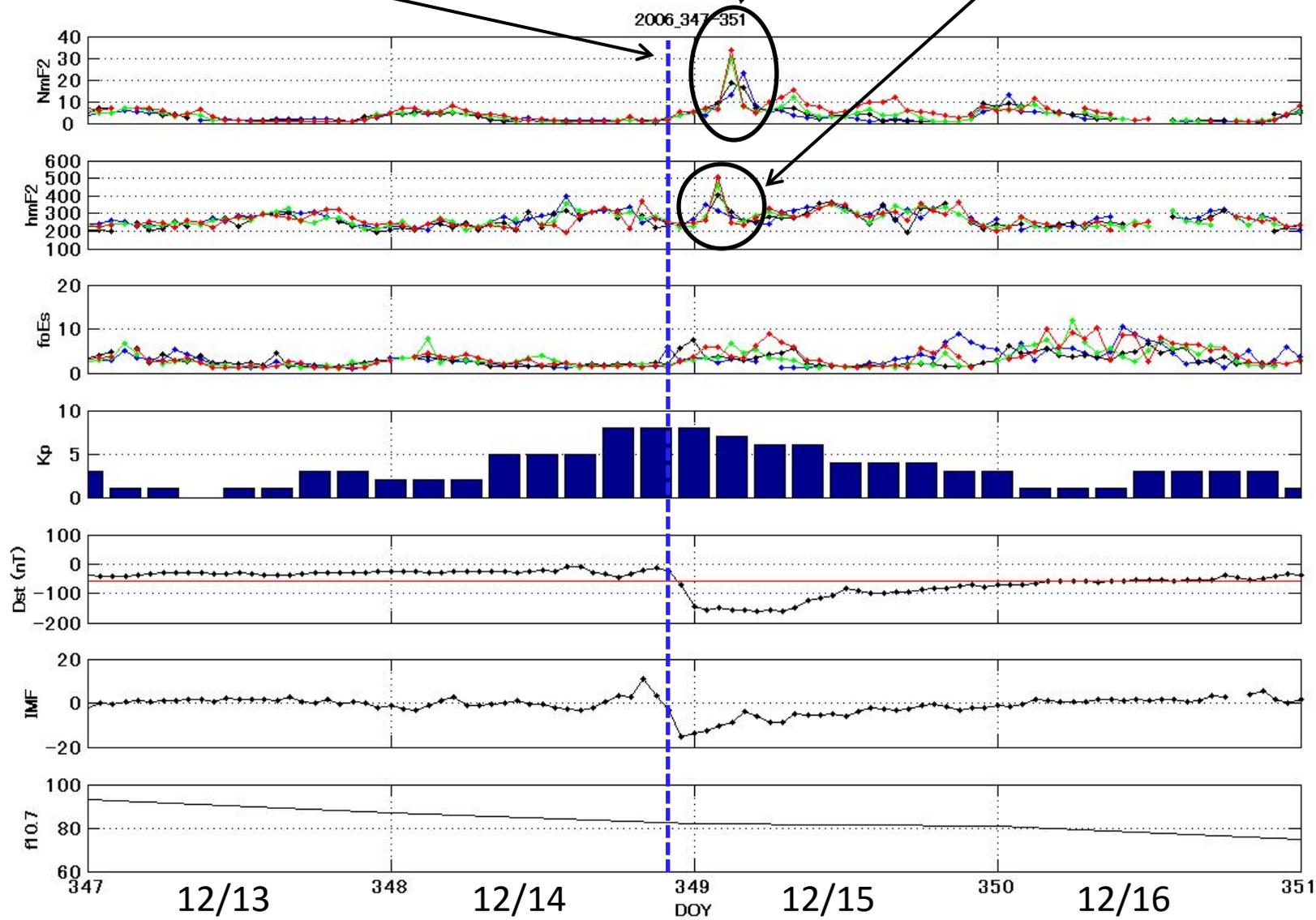
2次元マップ作成

# An example of magnetic storm period

NmF2急増 (12/15, 12:00 LT)

Storm onset (2006/12/14, 7:00 LT)

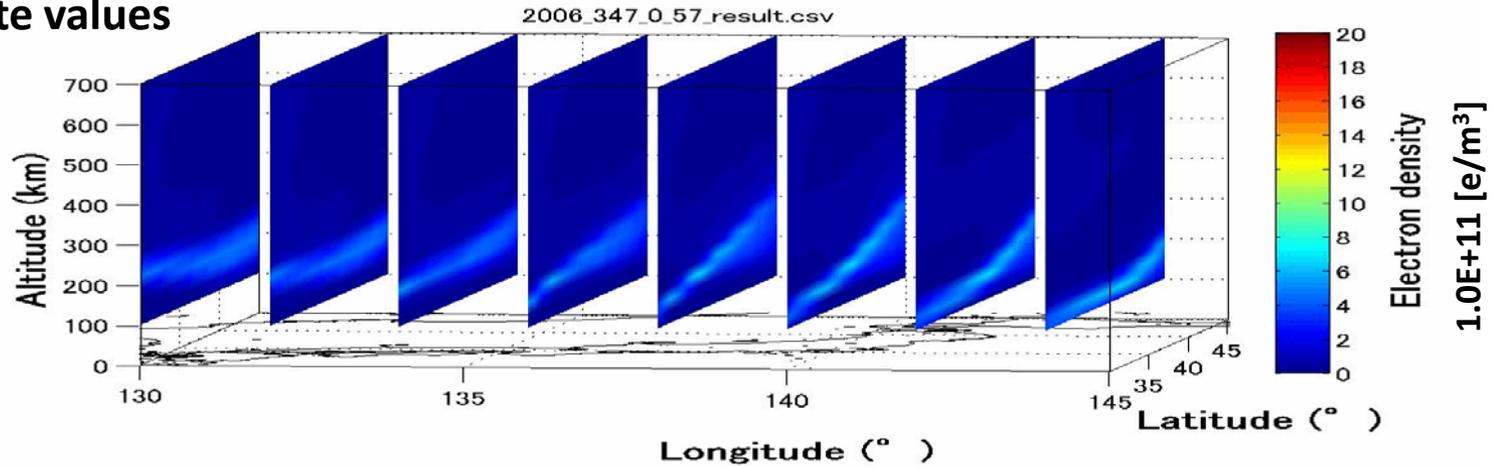
hmF2上昇 (2006/12/15, 11:00 LT)



Blue : Wakkanai, Black : Kokubunji, Green : Yamagawa, Red : Okinawa

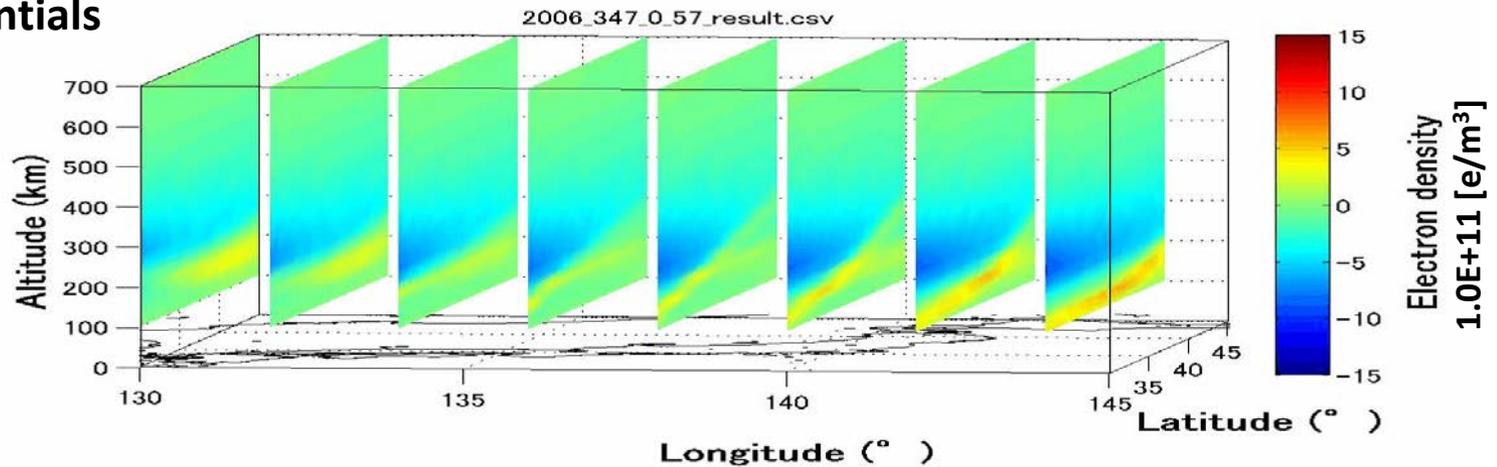
# Storm発生前後の変化 (2006/12/13 - 12/15)

## Absolute values

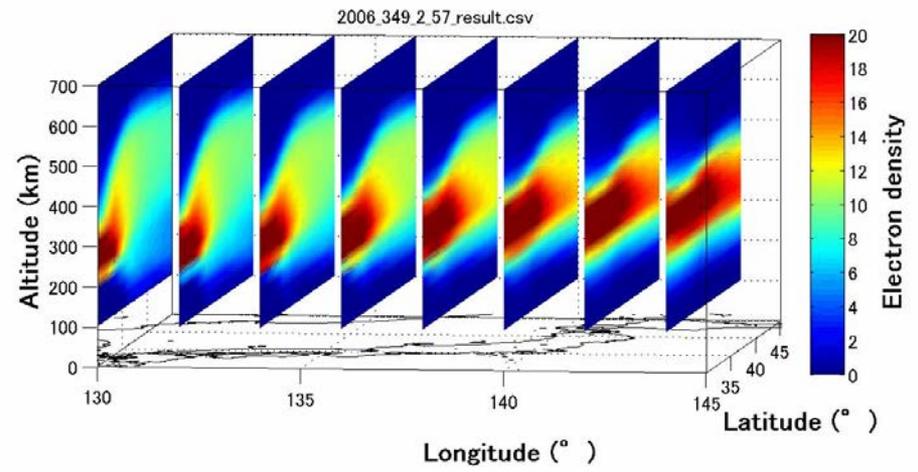
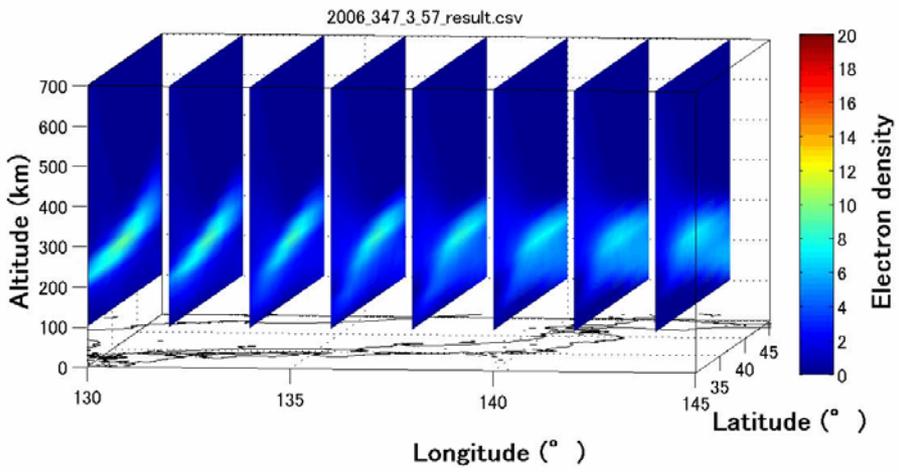


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## Differentials

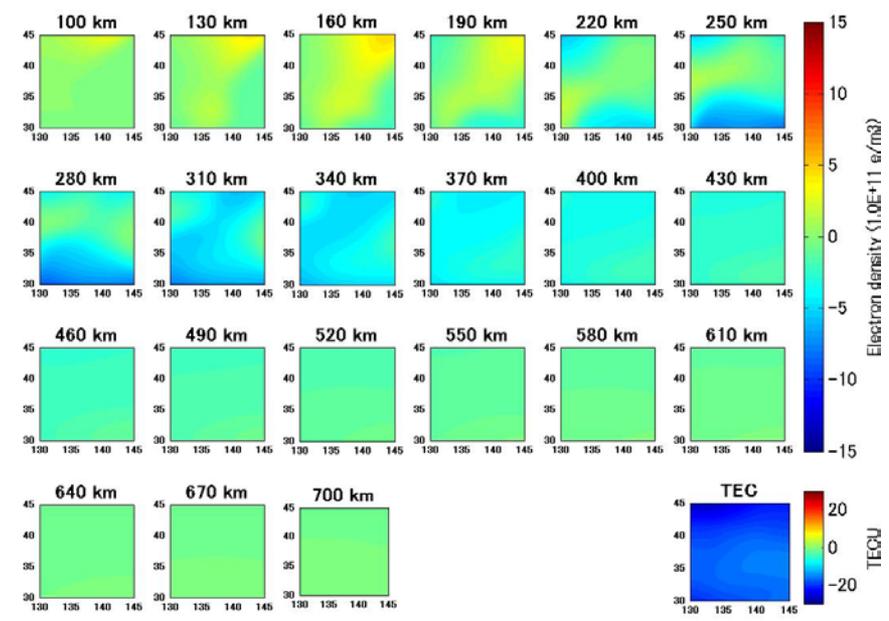


# Before Storm (2006/12/13, 13 LT) 5 hours after the main phase (2006/12/15, 12 LT)

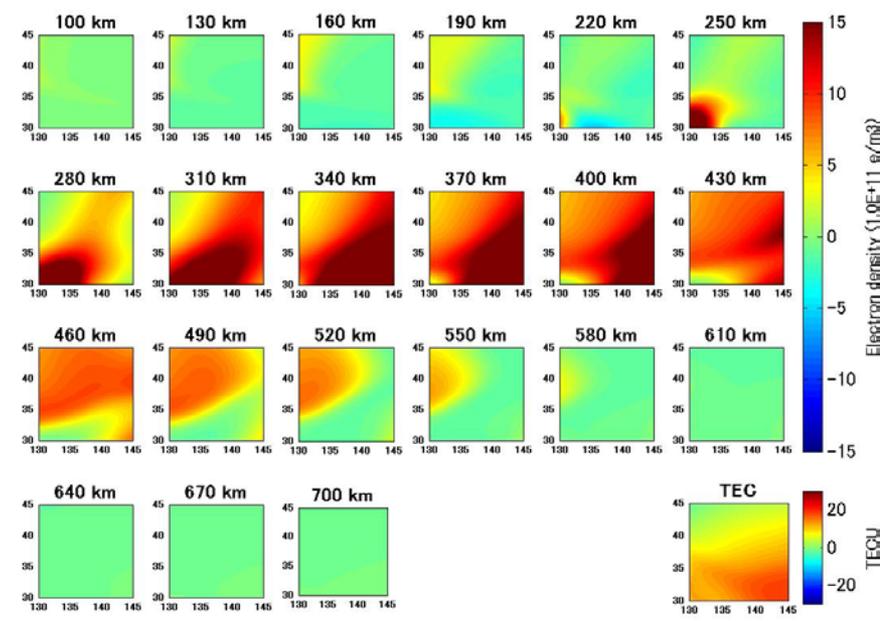


## 高度別断面(差分値像)

2006\_347\_3\_57\_result.csv



2006\_349\_2\_57\_result.csv



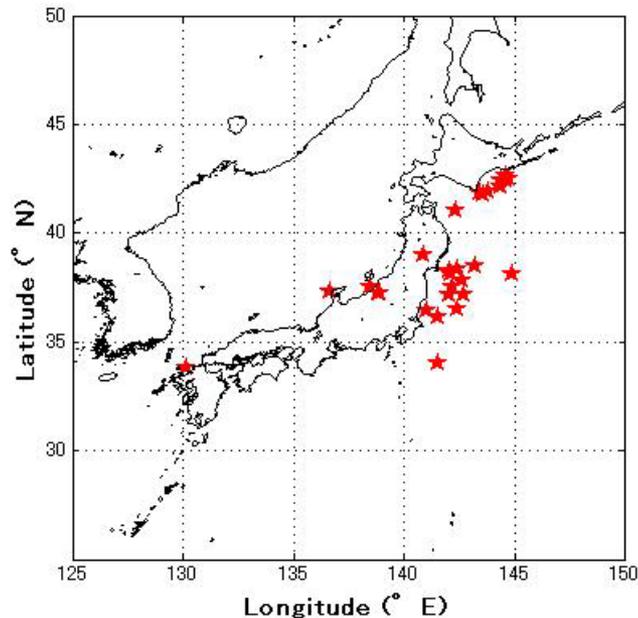
# Tomographic results for other EQs ( $M \geq 6.0$ , $D \leq 40$ km around Japan)

EQ with  $M \geq 6.0$ ,  $D \leq 40$  km over 1998-2010 + The 2011 Tohoku EQ ( $M 9.0$ )

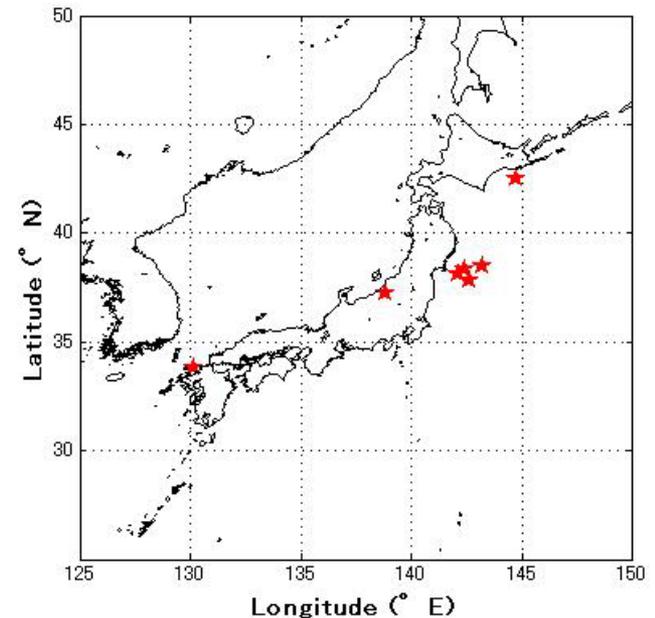
••• Total 53

GIM-TEC* Anomaly	Number of EQ
① Number of EQ with GIM-TEC* anomalies within 7 days before the EQ satisfied the condition	28
② Number of EQ with duration more than 10 hours/day in the case of ①	7

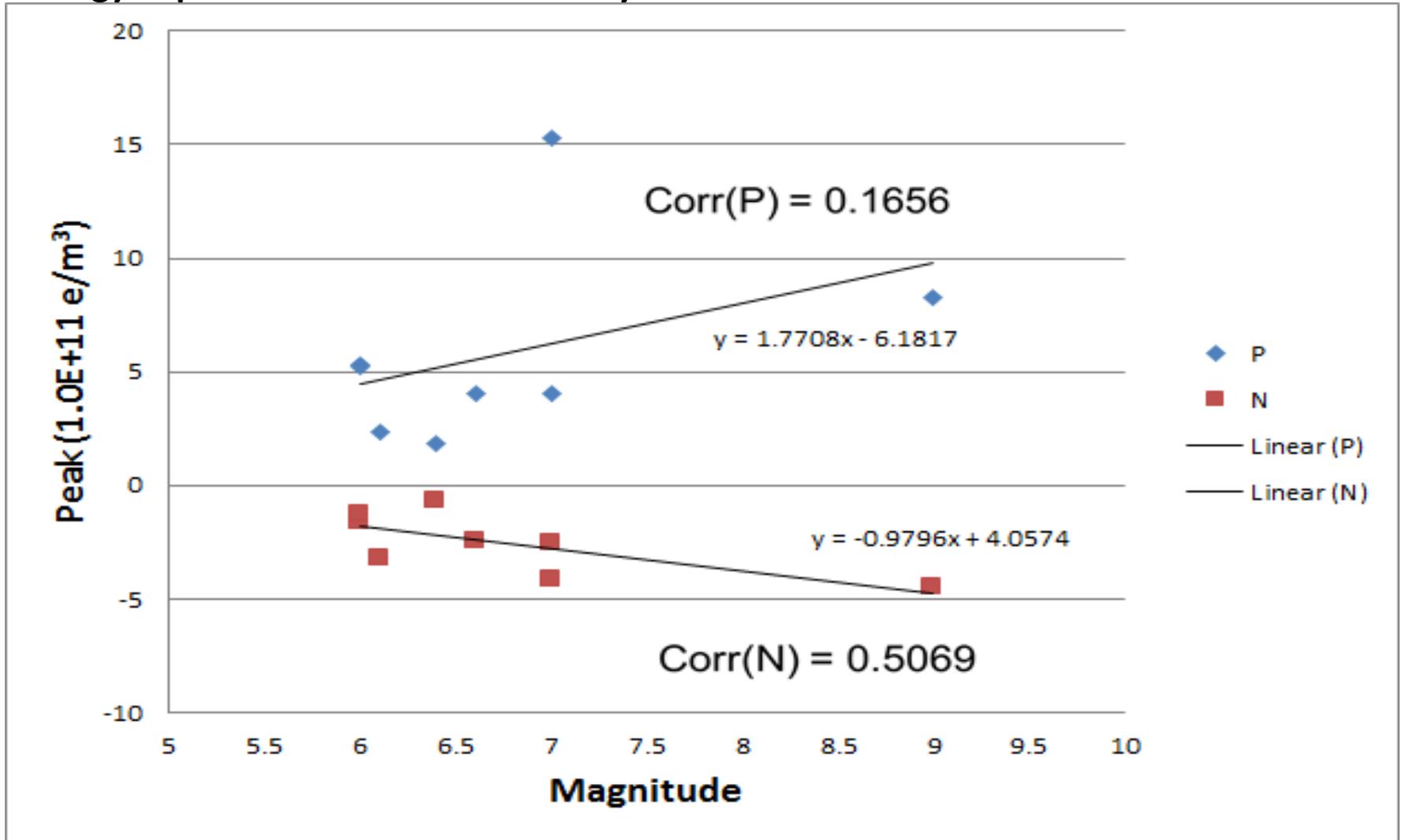
① Distribution on EQ of ① (28 EQ)



② Distribution on EQ of ② (7EQ)



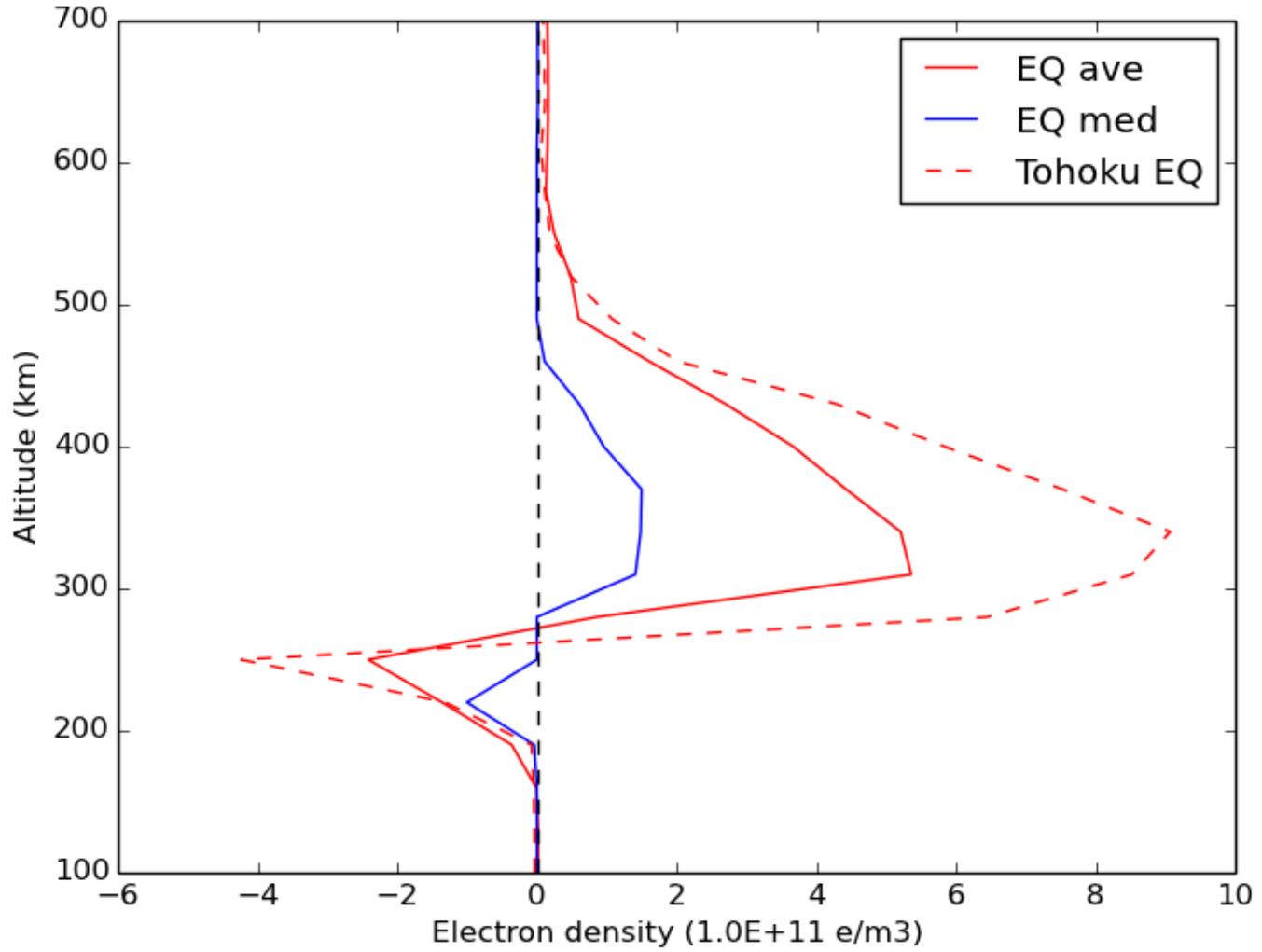
# Energy dependence of electron density enhancement



Energy at surface above the hypocenter

$$E = \frac{10^{4.8+1.5M}}{Depth^2}$$

# Difference of electron density profile from the 15 days backward median profile over epicenter

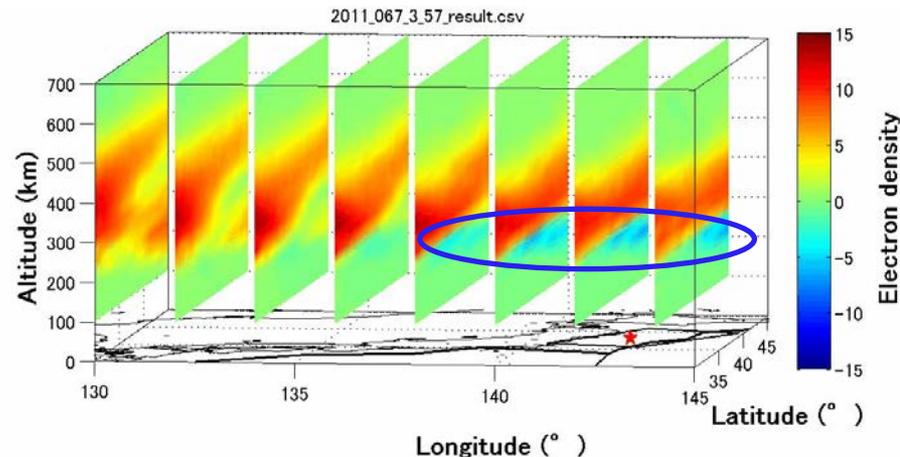


# Summary for Tomographic approach

GIM-TEC\*  $\Rightarrow$  Significant positive anomaly

Characteristics of 3 D structure

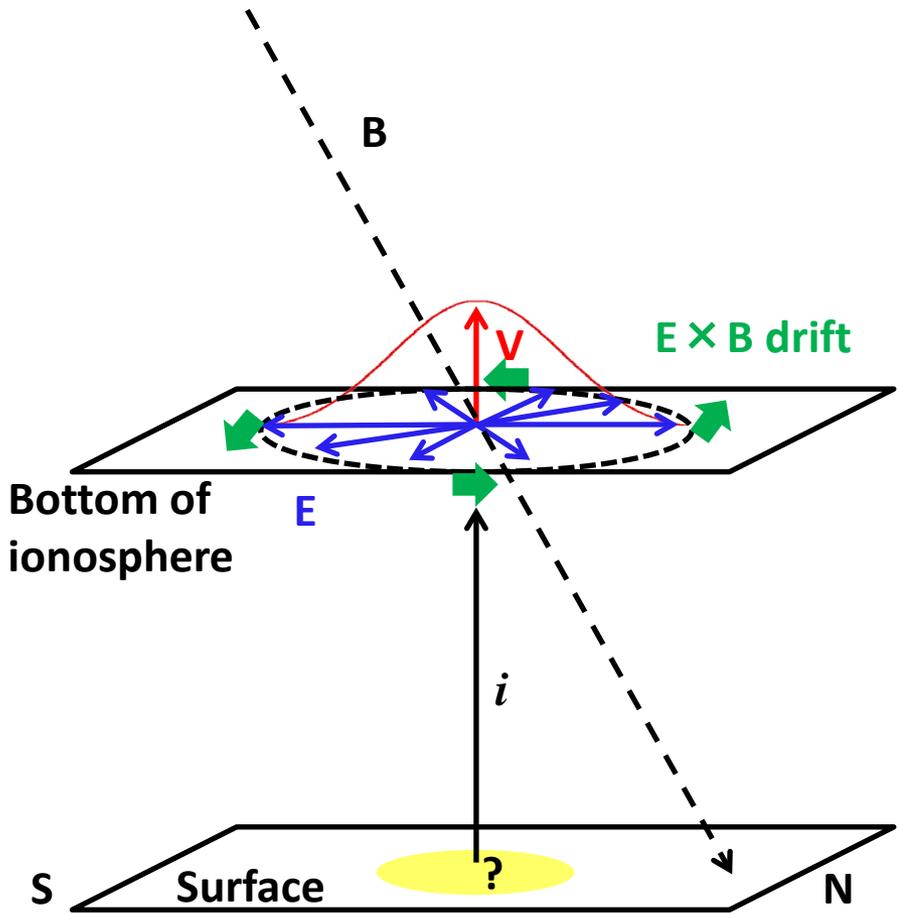
- Local decrease of electron density around 250 km height over the epicenter region.
- increase of electron density at the higher altitude.
- 6/7 of the EQ with a longer GIM-TEC\* anomaly (10 hours/day ) shows the typical 3D structure (see below) 1-7 days before the EQ.



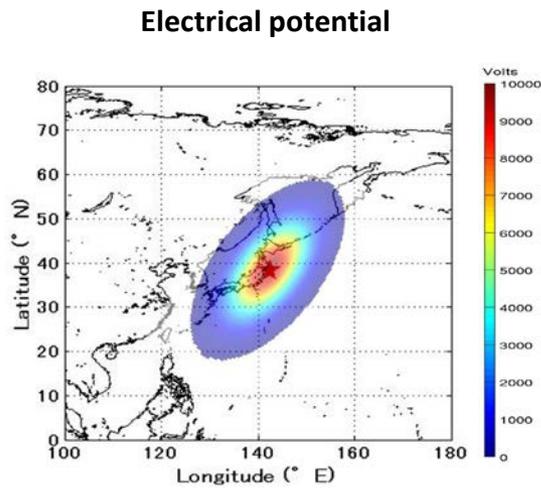
The typical 3 D structure preceding longer GIM-TEC\* anomaly

# Evaluation with numerical simulation for electron density changes before the EQ

- potential increase at the lower ionosphere

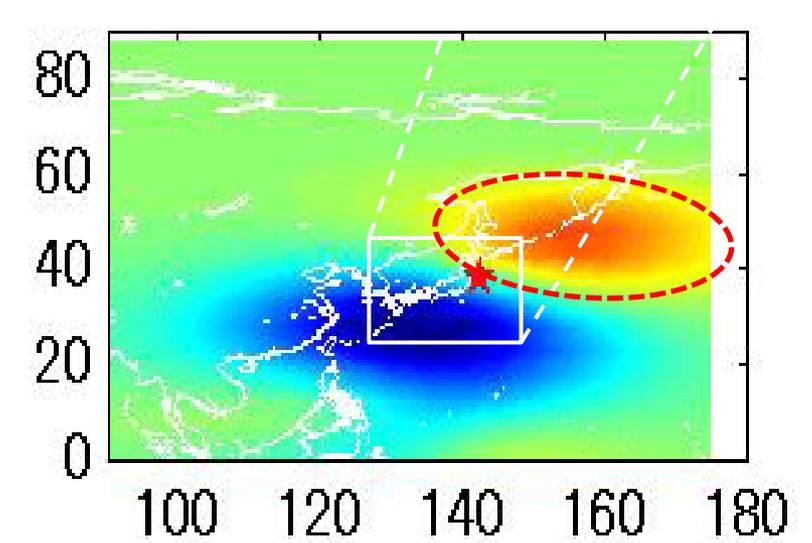
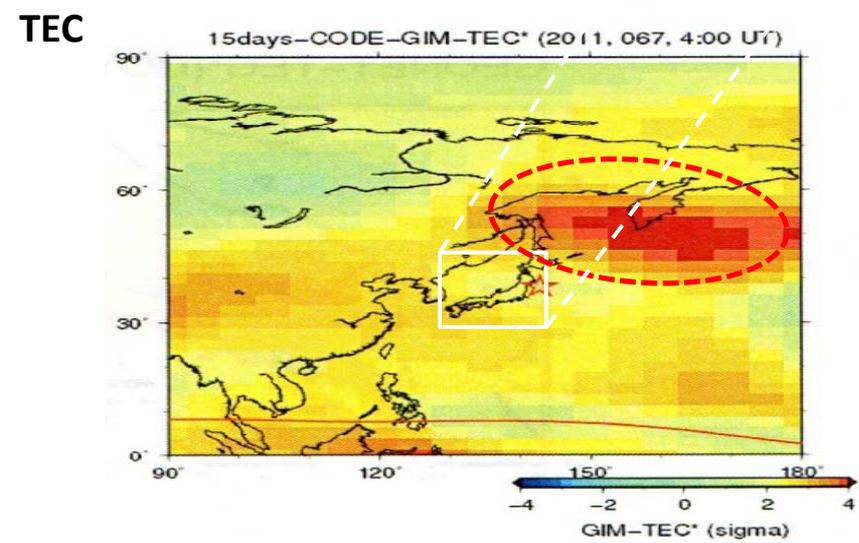
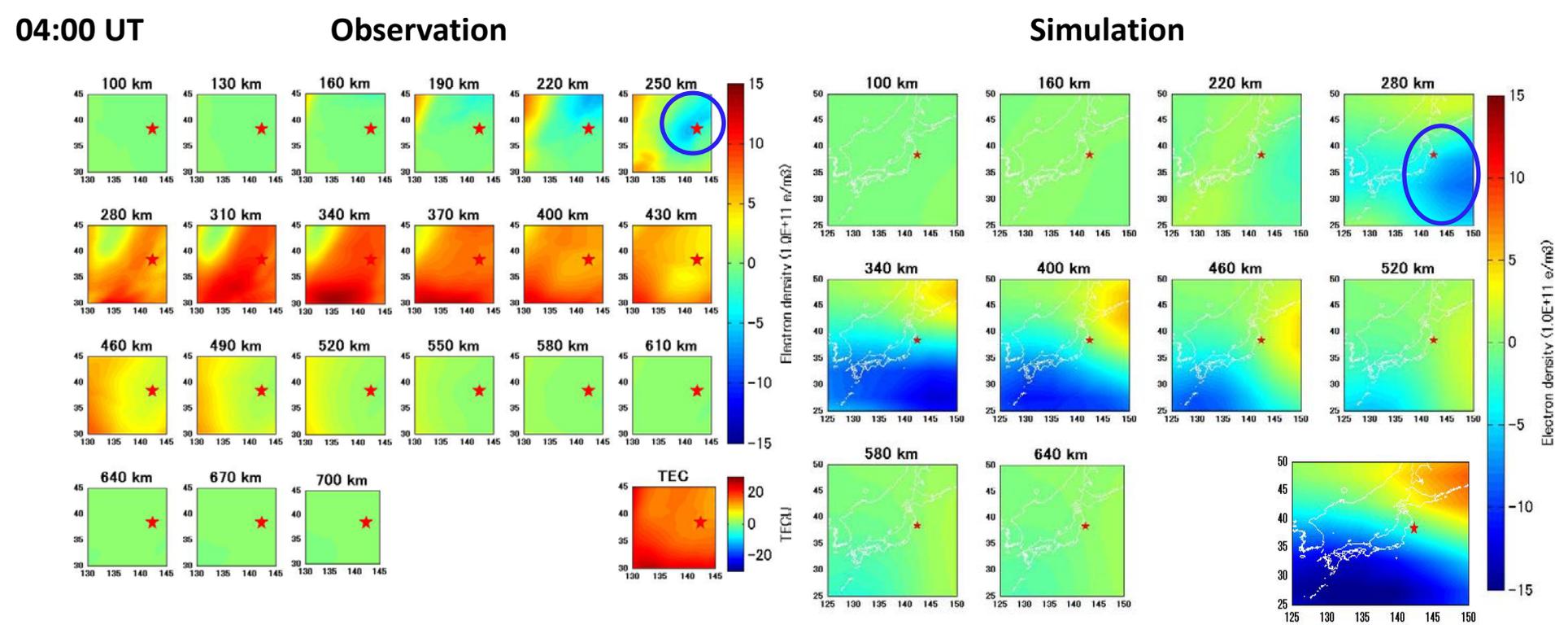


Thermosphere-Ionosphere-Electrodynamics  
General Circulation Model (TIE-GCM) : NCAR



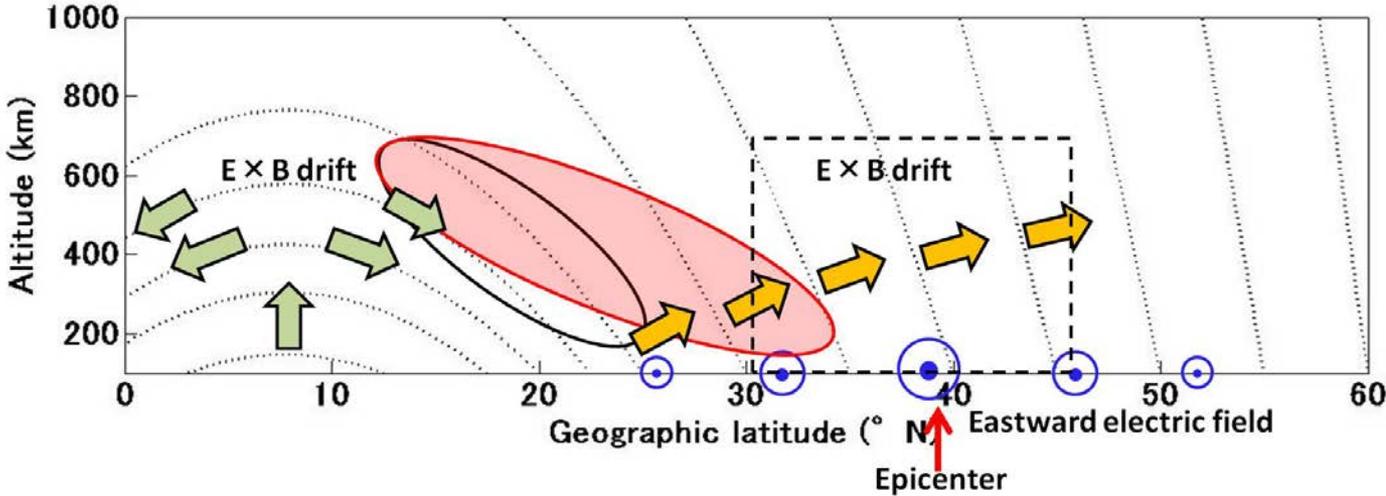
- march 8, 2011
- 10000 V at 97 km height (10 mV/m)
- Onset of the additive potential is at 0:00 UT and the intensity does not change.

✂ personal communication : I-T. Lee, NCU, NCAR



“electron density increase at altitude of 280~430 km”, and “TEC increase over Japan”

▪ Additive eastward electric field



Electrons move upward and northward due to  $E \times B$  drift.



Keep the high electron density due to low collision rate at higher altitude



Increase of electron density and TEC

▪ Equator-ward neutral wind

▪ less evidence of TEC variation from north to south

# Summary

- Investigation on Ionosphere (electron density/TEC) is useful for EQ precursor study .
- For Japan area, positive (increase) TEC anomalies are significant in statistical study and there are epicentral and magnitude dependences.
- Lead time is likely to be less than 5 days and the disturbed area looks wide for EQ-related TEC anomalies .
- Tomographic analysis show that Local decrease of electron density around 250 km height over the epicenter region increase of electron density at the higher altitude and 6/7 of the EQ with a longer GIM-TEC\* anomaly (10 hours/day ) provides the typical 3D structure before the EQ.
- Tomographic approach is essentially important to clarify the mechanisms.

**Thank you for attention**